A design approach to determine the shear capacity of reinforced concrete beams shear

strengthened with NSM systems

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Abstract

This paper present a design approach to predict the shear capacity of reinforced concrete (RC) beams strengthened

with fiber reinforced polymer (FRP) laminates/rods applied according to the near surface mounted (NSM) technique.

The new approach is based on the simplified modified compression field theory (SMCFT) and considers the relevant

features of the interaction between NSM FRP systems and surrounding concrete, like debond and concrete fracture.

In the SMCFT model, the shear strength of a RC element is a function of two parameters: the tensile stress factor in

the cracked concrete (β), and the inclination of the diagonal compressive stress in the web of the section (θ).

However, this approach is not a straightforward design methodology due to its iterative nature.

A sensitivity analysis is carried out to assess the relative importance of each input parameter that mostly affect the

shear capacity of RC beams shear strengthened according to the NSM technique. Taking into account the obtained

results, equations to determine β and θ without recurring to an iterative procedure are derived. The experimental

results of 112 beams shear strengthened with NSM FRP are used to appraise the predictive performance of the

developed approach. By evaluating the ratio between the experimental results and the analytical predictions, an

average value of 1.14 is obtained, with a coefficient of variation of 13.1%, being safe estimations 87% of the

predictions.

Keywords: Reinforced concrete beams; Shear strengthening; Fiber Reinforced Polymer; Simplified Modified

Compression Field Theory; Sensitivity Analysis; Monte Carlo simulation.

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Introduction

The prediction of the shear capacity of reinforced concrete (RC) beams is a challenging task because shear mobilizes several complex resisting mechanisms such as: i) shear resistance assured by the uncracked concrete in the compression zone; ii) interface shear transfer by aggregate interlocking in the cracked concrete; and iii) dowel action of the longitudinal reinforcement (Bellamkonda 2013). There are two prominent approaches that have been used to predict the shear strength of RC beams with and without shear reinforcement: Truss Model (TM) and Modified Compression Field Theory (MCFT).

Truss model (TM) is based on the following two assumptions: 1) the diagonal compression struts, before and after concrete cracking are inclined at an angle of 45 degrees to the longitudinal axis of the RC member; 2) the concrete tensile strength is negligible. Hence, the truss model predicts conservative values for the ultimate shear strength of the RC elements (Blanksvärd 2009). ACI (2011) and EuroCode2 (2001) are based on the truss model. In ACI, the inclination of the concrete crack is assumed 45 degrees but does not neglect the tension in the concrete, while the EuroCode2 neglects the tension but suggests a range of angle values for the shear crack inclination (21.8 and 45 degrees).

The Modified Compression Field Theory (MCFT) was developed by Vecchio and Collins (Vecchio and Collins 1986) by taking into account the resisting contribution of cracked RC member in tension. By applying this theory for the prediction of the shear strength of 102 panels tested experimentally, an average predictive level of 1.01 (ratio between experimental and model results), with a coefficient of variation (COV) of 12.2%, was obtained (Bentz *et al.* 2006). Nevertheless, solving the equations of the MCFT to evaluate shear capacity of a RC member requires an iterative procedure and the knowledge of a relatively high number of parameters, which introduces extra difficulties in the designer perspective. AASHTO LRFD (2014) is based on MCFT model.

Bentz *et al.* (2006) proposed a simplified approach of the MCFT (SMCFT) method. In this model, the shear strength of a section is a function of two parameters: the tensile stress factor in the cracked concrete (β), and the inclination of the diagonal compressive stress in the web of the section (θ). In spite of the simple format of the equations for β and θ , the method provides excellent predictions of shear strength of RC beams. By adopting the SMCFT, an average ratio of experimental to predicted shear strength of 1.11, with a COV of 13.0%, was obtained when applied to 102 RC specimens tested experimentally (Bentz *et al.* 2006).

Recently, Bianco *et al.* (2010) suggested a new formulation to predict the contribution of near surface mounted (NSM) carbon fiber reinforced polymer (CFRP) laminates/rods for the shear strengthening of RC beams. NSM technique with CFRP laminate/rod is an effective strengthening technique for the shear strengthening of RC beams. According to this technique, slits are opened on the concrete cover of the beam's lateral faces, filled with an adhesive (in general of epoxy type), and CFRP laminate/rods are inserted into these slits (De Lorenzis and Nanni 2001, Barros and Dias 2010). This technique requires no surface preparation, and after opening the slits on the lateral concrete cover, minimum installation time is required (Barros and Dias 2010).

One of the input parameters in Bianco et al. approach is the inclination of the critical diagonal crack (CDC), θ . However, due to lack of an appropriate approach to predict the θ , this model gives conservative estimates of the shear strength contribution of NSM systems. This model was applied to an experimental program formed by 72 RC beams, and an average ratio of the predictions versus the experimental values of 0.69, with a COV of 42%, was obtained (Bianco *et al.* 2014).

In the present paper a new model is presented to predict the shear capacity of typical RC building beams shear strengthened with FRP laminates/rods applied according to the NSM technique (where crack spacing less than 300 mm is expected to occur). The new technique is based on the SMCFT and Bianco *et al.* formulations. To assess the relative importance of each input parameter that affects the shear capacity of RC beams strengthened with FRP, the tensile stress factor in cracked concrete (β), and the inclination of the diagonal compressive stress in the web of the section (θ), a sensitivity analysis is carried out. Based on the results, equations for obtaining β and θ without recurring to any iterative procedure were derived.

To assess the predictive performance of the proposed analytical formulation (Baghi, Barros, and Bianco (BBB)), a database (DB) composed of 112 experimental results of RC beams shear strengthened with NSM FRP systems was set from published literature. The performance of the BBB is appraised using the collected data registered in the DB.

The proposed model (BBB)

A new shear design approach is developed to predict the shear capacity of RC beams shear strengthened with FRP laminates/rods applied according to the NSM technique. The new approach is based on the SMCFT and considers the relevant features of the interaction between NSM FRP laminates/rods and surrounding concrete, like debond and concrete fracture (Baghi 2015). The new model is based on combining the formulation of NSM technique, suggested

by Bianco *et al.* (Bianco *et al.* 2014), with the simplified MCFT, to which it is attributed the acronym BBB. According to the BBB model, the shear capacity of a NSM-FRP shear strengthened RC element is obtained from the following equation:

$$v = v_c + v_s + v_f = \beta \sqrt{f_c} + \rho_{sy} f_{y \text{ yield}} \cot \theta + v_f$$
 (1)

where v is the shear stress and is assumed to be constant over the cross section, thus $v = \frac{V}{db_w}$, f_c is the concrete compressive strength, ρ_{sy} and f_{yyield} are the ratio and the yield stress of the transverse steel reinforcement, respectively. d and b_w are effective depth and width of the beam, respectively. In Eq. (1), β and θ are the tensile stress factor in the cracked concrete (β) and the inclination of the diagonal compressive stress in the web of the section (θ), determined from Eq. (2) and Eq. (3), respectively.

$$\beta = \frac{0.4}{1 + 1500\varepsilon_{x}} \frac{1300}{1000 + s_{xx}} \tag{2}$$

$$\theta = \left(29 + 7000\varepsilon_{x}\right) \left(0.88 + \frac{s_{xe}}{2500}\right) \le 75^{\circ}$$
(3)

where

$$s_{xe} = \frac{35s_x}{a_v + 16} \ge 0.85s_x \tag{4}$$

representing physically the crack spacing, where s_x and a_g are the vertical distance between longitudinal reinforcement and the maximum dimension of aggregates, respectively. If the longitudinal reinforcement is not yielded, Eq. (5) can be used to calculate the ε_x :

$$\varepsilon_x = \frac{f_{sl}}{E_{sl}} = \frac{v \cot \theta - v_c / \cot \theta}{E_{sl} \rho_{sl}}$$
 (5)

otherwise $\varepsilon_x = \varepsilon_{sly}$, where E_{sl} , ρ_{sl} , and ε_{sly} are the modulus of elasticity, longitudinal reinforcement ratio and yield strain of this reinforcement, while v_c and v are the shear strength of concrete and of the RC member, respectively. The shear strength contribution provided by a system of NSM FRP laminate/rod (v_f) is determined by Bianco *et al.* (2014).

Bianco et al. (2014) proposed a 3D mechanical model to predict the shear strength contribution of NSM CFRP laminates/rods. The mode of failure of an NSM FRP laminate/rod subjected to an imposed end slip can be categorized into four groups: debonding, tensile rupture of laminate, concrete semi-pyramid tensile fracture, and a mixed shallow semi-pyramid plus debonding failure mode (Fig. 1e).

During the loading process of a RC beam, when the concrete average tensile strength is attained at the bottom part of the web, some shear cracks originate, and successively progress towards the flange of the beam. These cracks can generate a single crack, Critical Diagonal Crack (CDC), with inclination of θ with respect to the beam longitudinal axis (Fig. 1a). At load step t_n , the two web parts become separated by the CDC and they start moving apart by rotating around the crack tip (point E in Fig. 1a). From that step, by increasing the applied load, the CDC opening angle $\gamma(t_n)$ progressively widens. The laminates that bridge the CDC offer resistance to its widening. The load imposed to the laminate, in consequence of the loaded end slip (δ_{Li}) evolution, is transferred by bond to the concrete surrounding the laminate along its effective bond length, L_{fi} that is the shorter length between the two parts into which the crack divides its actual length. The following paragraphs introduce the formulation of this approach:

Step 1: Determine the average available resisting bond length ($\bar{L}_{R/l}$) and the minimum integer number of FRP reinforcements that cross the CDC ($N_{f,\text{int}}^l$) (Fig. 1a):

$$\overline{L}_{Rfi} = \frac{h_w \sin \theta (\cot \theta + \cot \theta_f)}{4 \sin(\theta + \theta_f)}$$
(6)

$$N_{f,\text{int}}^{l} = round \left[h_{w} \frac{\cot \theta + \cot \theta_{f}}{s_{f}} \right]$$
(7)

Step 2: Evaluation of various constants (Fig. 1c and 1d):

There are three types of constants:

1) Geometric constants:

Perimeter of FRP cross section (L_p), cross sectional area of the relevant surrounding concrete prism (A_c), and CDC length (L_d):

$$L_p = 2b_f + a_f \; ; \; A_c = s_f \frac{b_w}{2} \; ; \; L_d = \frac{h_w}{\sin \theta}$$
 (8)

2) Mechanical constants:

The ultimate tensile force of FRP reinforcement (V_f^r), concrete average tensile strength (f_{ctm}), and concrete Young's modulus (E_c):

$$V_f^{tr} = a_f b_f f_{fu} (9a)$$

$$f_{ctm} = 0.3(f_c' - 8)^{2/3} \tag{9b}$$

$$E_c = 9979(f_c')^{1/3}$$
 (9c)

3) Bond-Modeling constants encompass:

Bond modeling constant (J_1), integration constant for the softening frictional phase (C_3), constant entering the governing differential equation for elastic phase (λ), effective resisting bond length (L_{Rfe}), and maximum value of force transferable through bond by the given NSM-FRP reinforcement (V_{f1}^{bd}):

$$J_{1} = \frac{L_{p}}{A_{f}} \left[\frac{1}{E_{f}} + \frac{A_{f}}{A_{c}E_{c}} \right] ; C_{3} = \frac{V_{f}^{"}J_{1}}{L_{p}\lambda} ; \frac{1}{\lambda^{2}} = \frac{\delta_{1}}{\tau_{b}J_{1}} ; L_{Rfe} = \frac{\pi}{2\lambda} ; V_{f1}^{bd} = \frac{L_{p}\lambda\delta_{1}}{J_{1}}$$

$$(10)$$

Step 3: Determine the reduction factor of the initial average available resisting bond length (η), and equivalent value of the average resisting bond length ($\bar{L}^{eq}_{R\bar{p}}$):

The average resistance bond length is determined from:

$$\overline{L}_{Rfi}^{eq} = \eta \ \overline{L}_{Rfi} \tag{11}$$

where:

$$\eta = \begin{cases}
\frac{f_{ctm}}{f_{ctm}} & \text{if } f_{ctm} < f_{ctm}^* \\
1 & \text{if } f_{ctm} \ge f_{ctm}^*
\end{cases}$$
(12)

with:

$$f_{ctm}^* = \frac{L_p \lambda \delta_1 \sin(\lambda L_{Rfi})}{J_1 \cdot \min(L_{Rfi} \tan \alpha, b_w / 2) \cdot \min(s_f \sin \theta_f, 2L_{Rfi} \tan \alpha)}$$
(13)

representing the concrete average tensile strength above which concrete fracture does not occur, where:

$$L_{Rfi} = \begin{cases} \overline{L}_{Rfi} & \text{if } \overline{L}_{Rfi} \le L_{Rfe} \\ L_{Rfe} & \text{if } \overline{L}_{Rfi} > L_{Rfe} \end{cases}$$

$$(14)$$

Step 4: Determine the value of imposed slip in correspondence of which the maximum force transmissible by \overline{L}_{Rfi}^{eq} is attained $(V_{fi}(\overline{L}_{Rfi}^{eq}; \mathcal{S}_{Li}))$:

$$\delta_{Lu} = \begin{cases} \delta_{L1} \left(\overline{L}_{Rfi}^{eq} \right) & \text{if} \quad V_{f1}^{db} < V_{f}^{tr} \\ \min \left[\delta_{L1} \left(\overline{L}_{Rfi}^{eq} \right); \delta_{Li} \left(V_{f}^{tr} \right) \right] & \text{if} \quad V_{f1}^{db} \ge V_{f}^{tr} \end{cases}$$

$$(15)$$

where $\delta_{L1}(\bar{L}^{eq}_{R\beta})$ is the value of imposed end slip in correspondence of which the bond-based constitutive law $V^{bd}_{fi}(\bar{L}^{eq}_{R\beta};\delta_{Li})$ attains the peak value:

$$\delta_{L1}\left(\overline{L}_{Rfi}^{eq}\right) = \begin{cases} \delta_{1}\left[1 - \cos\left(\lambda \overline{L}_{Rfi}^{eq}\right)\right] & \text{if } \overline{L}_{Rfi}^{eq} \leq L_{Rfe} \\ \delta_{1} & \text{if } \overline{L}_{Rfi}^{eq} > L_{Rfe} \end{cases}$$

$$(16)$$

and $\delta_{Li}(V_f^n)$ is the imposed end slip in correspondence of which the strip tensile strength is attained (V_f^n) :

$$\delta_{Li}\left(V_f^{tr}\right) = \delta_1 \left\{ 1 - \cos\left[-\arcsin\frac{C_3}{\delta_1}\right] \right\} \tag{17}$$

Step 5: Determine the maximum effective shear capacity $V_{fi,eff}^{\max}$ of the NSM-FRP reinforcement with equivalent average resisting bond length \overline{L}_{Rfi}^{eq} . The $V_{fi,eff}^{\max}$ is evaluated by neglecting the post-peak behavior of the constitutive law:

$$V_{fi,eff}^{\text{max}} = \frac{\delta_1 A_2}{2L_d A_3 \gamma_{\text{max}}} \left[\frac{\pi}{2} - \arcsin \psi - \psi \sqrt{1 - \psi^2} \right]$$
(18)

where:

$$A_{2} = \frac{L_{p}\lambda}{J_{1}} \; ; \; A_{3} = \frac{\sin(\theta_{f} + \theta)}{2\delta_{1}} \; ; \; \gamma_{\max} = \frac{2\delta_{Lu}}{L_{d}\sin(\theta_{f} + \theta)} \; ; \; \psi = 1 - A_{3}.\gamma_{\max}.L_{d}$$
 (19)

Step 6: Determine the shear strength contribution provided by a system of NSM-FRP reinforcements:

$$V_f = 2N_{f,\text{int}}^l V_{fi,\text{eff}}^{\text{max}} \sin \theta_f \tag{20}$$

$$v_f = 2N_{f,\text{int}}^l V_{fl,eff}^{\text{max}} \sin \theta_f / (b_w d)$$
(21)

Figure 2 presents the solution procedure to calculate the shear strength of a RC beam according to the BBB. In case of FRP rods, $a_f = b_f = \sqrt{\pi} \, D_f / 2$, $A_f = \pi D_f^2 / 4$, and $L_p = \pi D_f$. The solution procedures based on BBB is available in Appendix A.

Sensitivity analysis

Sensitivity analysis means to evaluate model output dependence (shear capacity of RC beams with and without strengthening system, Eq. (1)) on the values adopted for the input parameters (h_w , b_w , a_f , b_f , s_f , θ_f , E_f , f_{fu} , α , τ_0 , δ_l , f_c , a_g , E_{sl} , f_{yyield} , ρ_{sl} , ρ_{sy}). Sensitive analysis can be useful for a range of purposes, such as: i) model simplification; ii) searching for errors in a model; and iii) uncertainty reduction (Saltelli *et al.* 2008).

There are two approaches to execute sensitivity analysis. The first approach is local sensitivity analysis, which is efficient for simple cost function. Local sensitivity analysis evaluates the model output by varying one input parameter in each running keeping the other parameters fixed. In this model the influence of the interactions between parameters on the cost function is neglected (MathWorks 2015). This type of analysis is not an appropriate approach for the BBB due to the iterative nature and complexity of this model. The other approach is the global sensitivity analysis (Monte Carlo analysis) (MathWorks 2015), where the output is evaluated by varying all the input parameters simultaneously (Gilman *et al.* 1998).

The Monte Carlo method, also called Monte Carlo analysis, is a process of running a model numerous times with a random selection of each input parameter simultaneously. There are always some errors involved with this technique, but this error can be decreased by increasing the number of random samples. Thanks to the continuous advance of computer processors, this approach is becoming quite attractive for determining the most influencing parameters in engineering models, and how they interact.

A sensitivity analysis was carried out to assess the relative importance of each input parameter on the shear capacity of the NSM-FRP shear strengthened RC beams (Eq. (1)) in order to figure out what are the input parameters that most affect the result. Based on the previous work (Bianco *et al.* 2014), all of the input parameters were characterized by a uniform probability distribution, which means a range of possible values with the same likelihood of occurrence (Table 1).

For sensitivity analysis, Eq. (1) was implemented in a spreadsheet that is re-calculated two hundred thirty thousand times, each time with a set of random new possible values of the input parameters. The number of samples (230000) was adopted after some preliminary study to reduce the computational time and error simultaneously.

The dimensionless r parameter, coefficient correlation, is used to measure the influence of each input parameter on the output variable (Eq. (1), β , and θ) (Fig. 3). The r is obtained from the following equation:

$$r = \frac{n\sum_{i=1}^{n} x_{i} y_{i} - (\sum_{i=1}^{n} y_{i})(\sum_{i=1}^{n} x_{i})}{\sqrt{n(\sum_{i=1}^{n} x_{i}^{2}) - (\sum_{i=1}^{n} y_{i}^{2}) - (\sum_{i=1}^{n} y_{i}^{2})^{2}}}}$$
(22)

where n is the number of the samples, x_i is the input parameter and y_i is output (value of BBB, β , and θ). The r parameter can varies between -1 and +1, where + and - signs are used for positive and negative linear correlations, respectively. Positive values of r indicate that when x increases, y also increases and when x decreases, y decreases. Negative values of r indicate that y decreases with the increase of x and y increases with the decrease of x. Finally y is close to 0 when no linear correlation or a weak linear correlation exists.

According to the results presented in Fig. 3, the input parameters that most affect the value of BBB, β and θ are the shear percentage of steel stirrups (ρ_{sy}), longitudinal steel reinforcement ratio (ρ_{sl}), the yield stress (f_{yyield}) of steel stirrups, the concrete compressive strength (f_c), ultimate tensile strength of FRP (f_{fu}), and shear percentage of FRP laminates/rods (ρ_f). As shown in Fig. 3b, the values of β and θ are also effected by the value of the angle (α) between axis and generatrices of the concrete fracture surface, the beam cross-section web's depth (h_w) and width (h_w), while the value of BBB is not significantly affected by these input parameters.

Figure 4 shows the relation between β vs $\frac{\rho_{sl}E_{sl}}{f_c'}$ and $\frac{\rho_{sy}f_{y\,yield}}{f_c'} + \frac{\rho_f f_{fu}}{f_c'}$ for more than 230000 generated samples with Monte Carlo simulation. In this figure, the surface that best fits the β vs x and y is presented. This surface is defined by the following equation:

$$\beta_s = -0.14 \times x^{0.21} + 0.13 \times y^{0.15} \qquad 0.05187 < \beta_s < 0.36$$
 (23)

where x and y are $\frac{\rho_{sy}f_{yyield}}{f_c} + \frac{\rho_f f_{fu}}{f_c}$ and $\frac{\rho_{sl}E_{sl}}{f_c}$, respectively. The surface is adopted after some preliminary fitting in terms of assuring surface objectivity of Goodness-of-Fit Statistics (MathWorks 2015). These statistics parameters are:

i) Sum of Squares due to Error (SSE), is the sum of the squares of residuals (Eq. 24). A small SSE indicates of tight fit of the model to the data;

$$SSE = \sum_{i=1}^{n} (y_i - f(x_i))^2$$
 (24)

where $f(x_i)$ is the value of the adopted function (surface or line) (x_i).

ii) R-square, is a number that indicates how well data fits a statistical model (Eq. 25), this statistic can take any value between 0 and 1, where a value equal to 1 indicates that the regression line fits perfectly the data;

$$R - Square = 1 - \frac{\sum_{i=1}^{n} (y_i - f(x_i))^2}{\sum_{i=1}^{n} (y_i - \overline{y})^2}$$
(25)

where \overline{y} is the mean value of y_i :

$$\overline{y} = \frac{1}{n} \sum_{i=1}^{n} y_i \tag{26}$$

iii) Root Mean Squared Error (RMSE), is an estimate of the standard deviation of the random component in the data (Eq. 27); an RMSE value closer to 0 indicates of tight fit of the model to the data.

$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} (y_i - f(x_i))^2}{n}}$$
(27)

More information about these Goodness-of-Fit Statistics can be found in (MathWorks 2015). The SSE, R-square, and RMSE for this fitted surface are 466, 0.374, and 0.046, respectively. In Eq. (23) $f_c^{'}$, f_{yyield} , f_{fu} , E_{sl} are in MPa. In this equation if the longitudinal Young's Modulus is not available, it can be assumed 200000 MPa. Furthermore, ρ_{sy} , ρ_f , and ρ_{sl} are introduced like ratio and not in percentage.

As mentioned, the shear strength of a concrete section is a function of β and θ . As shown in Fig. 5 for more than 230000 generated samples with Monte Carlo simulation, these two parameters are interdependent (Bentz *et al.* 2006; Baghi 2015). In the present work this interdependence is assumed, and Eq. (28) is suggested for obtaining θ_s from β_s :

$$\theta_s = 3.36 \times \beta_s^{-0.82} + 21.5$$
 $29^\circ \le \theta_s \le 60^\circ$ (28)

The SSE, R-square, and RMSE for this fitted curve are 155000, 0.9714, and 0.8354, respectively. In Fig. 4 the results are fitted for 2 variables (x and y), but in Fig. 5 the results are fitted for just one variable. Hence, it is reasonable the R-square value for β_s is not so good as the one of θ_s .

Assessment of the predictive performance of the developed model

A database (DB) containing 112 experiments are used to appraise the predictive performance of the developed approach (De Lorenzis and Nanni 2001; Dias 2008; Dias and Barros 2008; Islam 2009; Rizzo and De Lorenzis 2009; Dias and Barros 2010; Rahal 2010; Chaallal *et al.* 2011; Dias and Barros 2011; Rahal and Rumaih 2011; Dias and Barros 2013; Baghi 2015). More experiments are available in the literature, however they are not included in this database because critical parameters are missing in their description. This DB includes beams of different size, different longitudinal and transverse steel reinforcement ratios, and different NSM CFRP shear strengthening configurations and ratios. All the beams in this DB failed in shear.

The DB contains values from experiments performed on 90 beams with T cross section, and 22 beams with rectangular cross section (Fig. 6a). From 112 beams, 87 beams are shear strengthened by CFRP laminate/rod (Fig. 6b). From the 87 beams, 31 are shear strengthened with CFRP rods, and the remaining by CFRP laminates (Fig. 6c). All the collected data are reported in Table 5.

The beams tested by Dias and Barros (2008; 2010; 2011; 2013) were of type T cross section with the same shear span to effective depth ratio (2.5), CFRP laminates, and epoxy adhesive. These beams differed on the amount of existing still stirrups ($\rho_{sy} = 0.1\%$ and 0.17%), percentage of longitudinal reinforcement ($\rho_{sl} = 2.8\%$ and 3.2%), and concrete compressive strength ($f_c = 18.6, 39.7, \text{ and } 31.1 \text{ MPa}$). These series were strengthened with different configurations of NSM laminates in terms of both inclination θ_f and spacing s_f . However, the series V and VI of these authors (Dias 2008) were formed by beams of a higher shear aspect ratio (3.3) and concrete average compressive strength ($f_c = 59.4 \text{ MPa}$).

Those beams were characterized by the following common geometric and mechanical parameters: $b_w = 180$ mm; $h_w = 300$ mm; $f_{fu} = 2952$ MPa (for the series I, II, III, IV) and $f_{fu} = 2848$ MPa (for the series V and VI); $E_f = 166.6$ GPa (for the series IV), $E_f = 174.3$ GPa (for the series III, V, and VI), and $E_f = 170.9$ GPa (for series I and II); $a_f = 1.4$ mm; $b_f = 9.5$ mm (for the series I, II, III, V and VI) and $a_f = 1.4$ mm; $b_f = 10$ mm (for series IV).

The beams tested by Chaallal *et al.* (2011) were of T cross section type, and were strengthened in shear by CFRP rods, and tested under three point bending. These beams were characterized by cross-section dimensions of $b_w = 152$ mm and $h_w = 304$ mm. Concrete had average compressive strength of 25 MPa and 35 MPa in the series I and II, respectively. CFRP rods of 9.5 mm diameter, with tensile strength of $f_{fu} = 1270$ MPa and modulus of elasticity of $E_f = 148$ GPa, were used.

The beams tested by De Lorenzis and Nanni (De Lorenzis and Nanni 2001) were of T cross section type, strengthened in shear with CFRP rods, and tested under four point bending. These beams were characterized by cross-section dimensions of $b_w = 150$ mm and $h_w = 305$ mm. The concrete had an average compressive strength of 31 MPa. CFRP rods of nominal diameter around 9.5 mm, with tensile strength $f_{fu} = 1875$ MPa and modulus of elasticity $E_f = 104.8$ GPa, were adopted. Two different percentages of steel stirrups were used ($\rho_{sy} = 0.0\%$ and 0.26%).

The beams tested by Rizzo and De Lorenzis (2009) were of rectangular cross-section type, strengthened in shear by either rods (NR) or laminates (NL), and tested under four point bending. These beams were characterized by cross-section dimensions of $b_w = 200$ mm and $h_w = 210$ mm. The concrete had an average compressive strength of 29.3 MPa. Round CFRP rods of 8 mm diameter, with tensile strength $f_{fu} = 2210$ MPa and modulus of elasticity $E_f = 145.7$ GPa, were used. The laminates had cross-section dimensions $a_f = 2.0$ mm and $b_f = 16.0$ mm, and mechanical properties of $f_{fu} = 2070$ MPa and $E_f = 121.5$ GPa.

The beams tested by Islam (2009) were of rectangular cross-section type, strengthened in shear with CFRP round rods and tested under four point bending. These beams were characterized by cross-section dimensions of $b_w = 254$ mm and $h_w = 305$ mm. The concrete had an average compressive strength of 49.75 MPa. Round CFRP rods of 9 mm diameter, with tensile strength $f_{fu} = 2070$ MPa and modulus of elasticity $E_f = 124$ GPa, were used.

The beams tested by Baghi (2015) were of rectangular and T cross-section type, strengthened in shear with CFRP laminates, and tested under three point bending. Rectangular beams were characterized by cross-section dimensions of $b_w = 150$ mm and $h_w = 300$ mm, while the T cross section beams had a cross section dimensions of $b_w = 180$ mm and $h_w = 400$ mm. In rectangular and T cross sections type of beams the length of monitored shear span, a, was 3.0 and 2.5 times the effective beam's depth, d, respectively. The concrete had an average compressive strength of 32.7

MPa. CFRP laminates of $a_f = 1.4$ mm; $b_f = 10$ mm, with tensile strength $f_{fu} = 2620$ MPa and modulus of elasticity $E_f = 150$ GPa, were used.

The RC beams tested by Rahal (2010) and by Rahal and Rumaih (2011) were of T cross-section, and were strengthened in shear by NSM bars or steel (their label includes a letter R) or CFRP (their label includes a letter F) and tested under four point bending. These beams were characterized by T cross-section dimensions of b_w =150 mm and h_w =400 mm. The ratio between the shear span and the beam effective depth was a/d =3.0. Concrete average compressive strength ranged from 36.2 MPa to 37.8 MPa. NSM FRP bars with 8 mm diameters, f_{fu} = 1900 MPa and E_f 124 GPa were used.

The RC beams tested by Cisneros *et al.* (2012) were of rectangular cross-section strengthened in shear by either bars (their label starts by B) or laminates (their label starts by S) and tested under three point bending. The cross-section dimensions of the beams were b_w =200 mm and h_w =350 mm. Each beam was tested twice at each end and the ratio between the shear span and the beam's effective depth was equal to a/d = 2.9 (Fig. B.8). Concrete average compressive strength ranged from f_{cm} =22.84 MPa to f_{cm} =29.11 MPa. The NSM FRP bars were characterized by 8 mm diameter, while the laminates had cross section dimensions of a_f =2.5 mm and b_f =15 mm. FRP mechanical properties were f_{fu} =2500 MPa and E_f =165 GPa.

The angle α is assumed equal to 28.5° for all the experimental programs. To define the local bond stress-slip relationship, the following values are assumed: $\tau_0 = 20.1$ MPa; $\delta_1 = 7.12$ mm (Bianco *et al.* 2014). When CFRP rods are used, the equivalent square cross-section is adopted in the calculations (Bianco *et al.* 2014). In the BBB model the aggregate size (a_n) is assumed 25 mm for all the experimental programs.

For the Baghi, Barros, and Bianco (BBB) model and the new Simplified BBB model, herein designated by SBBB, the obtained values of $V_{ana.}$ are compared with $V_{exp.}$ of the DB, and the values of the λ factor corresponding to the $V_{exp.}/V_{ana.}$ ratio are included in Table 2 and represented in Fig. 7. In the BBB approach the average value of $V_{exp.}/V_{ana.}$ is 1.09, with a COV of 11.0%. This approach provided 82% safe estimations and 18% overestimations. The new model, SBBB, has assured an average value of $V_{exp.}/V_{ana.}$ of 1.14 with COV of 13.1%, composed of 86.6% of safe estimations and 13.4% overestimations.

A systematic trend in the error can be highlighted if the results are plotted in non-dimensional form, as it is shown in Fig. 8, where the shear resistance is normalized by a force dimensional parameter $b_w df_c$. In this figure, two lines limiting to $\pm 25\%$ the deviation of the predicted values from the experimental values are also represented, and it is verified that 91% of the results are inside of these bounds.

The values of λ are also classified according to the modified version of the Demerit Points Classification (DPC) (Moraes Neto *et al.* 2014) proposed by Collins (2001), where a penalty (PEN) is assigned to each range of λ parameter according to Table 3, and total of penalties (Total PEN) determines the performance of each analytical approach. According to the results included in Table 4, the predictive performance of BBB model is better than SBBB, since the former approach has a large number of predictions in the appropriate safety interval according to the DPC (Table 3), $\lambda \in [0.85-1.15[:69 \text{ samples with the BBB and 53 samples with the SBBB. However, the gain in design simplicity when SBBB is adopted seems to justify the increase in the conservative predictions (<math>\lambda \in [1.15-2[):55 \text{ and } 39 \text{ samples}$ when using the SBBB and BBB model, respectively. It is of upmost relevance to verify that both BBB and SBBB do not have predictions on the extremely dangerous and extremely conservative intervals.

Figure 9a presents the influence of the $\rho_{sl}E_{sl}$ / f_c on the predictive performance of the studied analytical models. As shown in this figure for SBBB, the average of the λ for R1 is in the appropriate safety interval, while for R2 and R3 is in the conservative interval. In the BBB model the λ is in the appropriate safety interval for all the three R ranges of values. According to SMCFT, the large ratio of longitudinal reinforcement decreases the ε_x (Eq. (5)), which increases β (Eq. (2)) and decreases θ (Eq. (3)). In fact the increase of the aggregate interlock resisting mechanisms due to this effect is not modelling directly in BBB model, but indirectly through the s_{xe} . Hence, Fig. 9a indicates the BBB model considers the effect of ε_x provided by longitudinal reinforcement on shear capacity of RC beams, while the SBBB is not considering so effectively the effect of the longitudinal reinforcement. The influence of $\rho_{xy}f_{yyield}$ / f_c on the λ parameter is represented in Fig. 9b. While in the BBB an almost constant λ parameters was obtained regardless the intervals of values adopted for $T = \rho_{xy}f_{yyield}$ / f_c parameter, in the SBBB model the λ parameter has the tendency to decrease with the increase of T. However, SBBB has only provided λ values in the conservative interval when applied to RC without steel stirrups, therefore for current situations where a certain percentage of steel stirrups exists, the SBBB is providing λ values in the appropriate safety interval.

Figure 9c presents the average of the λ parameter regarding to four classifications of F= $\rho_f f_{fu} / f_c$ as defined in this figure. For F smaller than 0.3, which includes the major part of the FRP shear strengthening interventions, the λ parameter obtained with the SBBB model is in the appropriate safety interval, while λ values in the interval of conservative predictions are determined for F above 0.3. Values of λ in the appropriate safety interval are obtained with the BBB model for all the ranges of values considered for the F parameter.

Conclusion

In this paper, a global sensitivity analysis (Monte Carlo simulation) was carried out for deriving, from known data, the equation to determine the values for two crucial parameters of the simplified modified compression field theory (SMCFT) used to estimate the shear capacity of reinforced concrete (RC) beams, namely, the tensile stress factor in cracked concrete (β), and the inclination of the diagonal compressive stress in the web of the section (θ). These equations were integrated into the SMCFT, which was coupled with an already published analytical formulation to derive a new approach (designated by SBBB) for the prediction of the shear capacity of RC beams shear strengthened with the near surface mounted (NSM) technique using fiber reinforcement polymer (FRP) systems.

Based on an extensive literature review regarding the shear strengthening of RC beams with FRP systems applied according to the NSM technique, a comprehensive database was assembled containing experimental results of 112 beams.

By evaluating the ratio between the experimental results and the analytical predictions ($\lambda = V_{\rm exp.}/V_{\it ana.}$), an average value of 1.14, with a COV 13.1% and 87% of safe estimations were obtained by using the SBBB. The developed approach is simple of using, quite convenient for design practice, and, conceptually, it can be extended to other FRP-based shear strengthening techniques, like the externally bonded reinforcement (EBR) and the embedded through section (ETS).

Appendix A

The procedure solution for one beam strengthened with NSM CFRP laminate (2S-4LI45-I (Dias and Barros 2010), Fig. 10) is herein explained:

BBB Approach:

Step 1: Assume a value for ε_x .

Step 2: Calculate the crack spacing based on Eq. (4).

Step 3: Calculate β (Eq. (2)) and θ (Eq. (3)).

Step 4: Calculate the shear strength based on Eq. (1).

Step 5: Calculate the longitudinal strain (Eq. (5)), ε_x , and compare to ε_x that was estimated in Step 1. Return to Step

1 with $\varepsilon_{_{X}}$ that has been calculated in Step 5 until $\left| \varepsilon_{_{X}}^{q+1} - \varepsilon_{_{X}}^{q} \right| / \varepsilon_{_{Y} \ yield} \le 10^{-6}$.

This procedure solution for the 2S-4LI45-I beam is presented in Table 6.

SBBB Approach:

Step 1: Calculate β_s and θ_s according to Eqs. (23) and (28), respectively.

Step 2: Calculate the shear strength based on Eq. (1).

This procedure solution for the 2S-4LI45-I beam is presented in Table 7. The inclination of the shear crack in the 2S-4LI45-I beam is presented in Fig. 11, that shows the BBB and SBBB can predict the crack inclination in reasonable accuracy.

Acknowledgments

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	Notation
A_f	Area of the strip's cross section
A_2	Integration constant entering the expressions to evaluate the $V_{\emph{fi,eff}}^{\max}$
A_3	Integration constant entering the expressions to evaluate the $V_{\emph{fi.eff}}^{\max}$
C_3	Integration constant for the softening friction phase
D_f	Diameter of FRP rod
E_c	Modulus of elasticity for concrete
E_f	Modulus of elasticity of FRP
E_{sl}	Modulus of elasticity of longitudinal reinforcement
$oldsymbol{J}_1$	Bond modeling constant
L_d	CDC length
L_p	Effective perimeter of the strip cross section
$L_{\!\scriptscriptstyle R\!fe}$	Effective resisting bond length

ith strip resisting bond length L_{Rfi} $ar{L}^{eq}_{Rfi}$ Equivalent average resisting bond length \overline{L}_{Rfi} Average available resisting bond length $N_{f,\text{int}}^l$ Equivalent average resisting bond length VShear force V_c Shear force in Concrete V_{f} Shear resistance contribution of fibers $V_{\scriptscriptstyle f}^{\scriptscriptstyle tr}$ Strip tensile rupture capacity Design value of the NSM shear strengthening contribution $V_{\scriptscriptstyle fd}$ Maximum effective capacity V_{f1}^{bd} Maximum value of force transferable through bond by the given FRP NSM system Shear resistance contribution of steel reinforcement Width of FRP laminate a_f Aggregate size a_{g} Thickness of FRP laminate b_f b_{w} Width of strengthened cross section d Effective depth Cylinder compressive strength of concrete f_c Value of concrete average tensile strength for values larger than which concrete fracture does not f_{ctm}^{τ} Concrete average tensile strength f_{ctm} Ultimate tensile strength of FRP f_{fu} Yield stress in reinforcement $f_{y \, yield}$ Beam web height h_w Number of samples n Coefficient correlation Horizontal distance between steel stirrup Spacing of NSM shear reinforcement S_f Distance between longitudinal reinforcement S_{x} Effective longitudinal crack spacing S_{xe} Shear stress v Shear stress in concrete V_c Shear stress in FRP laimates/rods v_f Shear stress in transverse reinforcement v_s Input parameter X_i Out put y_i \overline{y} Mean value of out put Angle defining the concrete fracture surface α Factor accounting for the tensile stress in the cracked concrete β Slip corresponding to the end of softening friction $\delta_{_{\! 1}}$

Imposed slip at the loaded extremity of the i^{th} strip

Imposed slip in correspondence of which the comprehensive peak force transmissible by $\bar{L}_{R\bar{p}}^{eq}$ is

 δ_{Li}

 δ_{Iu}

attained

$\delta_{\!\scriptscriptstyle L1}$	Value of δ_{Li} defining the end of the first phase of the bond-based constitutive law
$oldsymbol{arepsilon}_f$	Effective tensile strain in FRP reinforcement
$\mathcal{E}_{_{\chi}}$	Longitudinal strain
$\gamma_{ m max}$	CDC opening angle for which the maximum effective capacity is attained
η	Reduction factor of the initial average available resisting bond length
λ	Constant entering the governing differential equation for elastic phase
θ	Direction of the principal stress/strain
$ heta_f$	Inclination of FRP laminates
$ ho_{\scriptscriptstyle f}$	Shear percentage of FRP laminate/rod
$ ho_{\scriptscriptstyle sl}$	Longitudinal steel reinforcement ratio
$ ho_{\scriptscriptstyle sy}$	Transverse steel reinforcement ratio
$ au_0$	Adhesive-cohesive initial bond strength
Ψ	Constant necessary to evaluate the maximum effective capacity provided by the equivalent average
	resisting bond length

References:

- AASHTO, L. R. F. D. (2014). Bridge Design Specifications., American Association of State Highway and Transportation Officials.
- ACI Committee & International Organization for Standardization (2011). Building code requirements for structural concrete (ACI 318-08) and commentary, American Concrete Institute.
- Baghi, H. (2015). The effectivness of SHCC-FRP panles of the shear resistance of RC beams. PhD Thesis, University of Minho.
- Bellamkonda, S. A. (2013). Modeling of Shear Strengthening of Reinforced Concrete Beams Retrofitted with Externally Bonded Fiber Reinforced Polymers. Master Thesis, Louisiana State University.
- Bentz, E. C., Vecchio, F.J., and Collins, M.P. (2006). "Simplified Modified Compression Field Theory for Calculating Shear Strength of Reinforced Concrete Elements." *ACI STRUCTURAL JOURNAL* 103: 614-624.
- Bianco, V., Barros, J.A.O., and Monti, G. (2010). "New approach for modeling the contribution of NSM FRP strips for shear strengthening of RC beams." *ASCE Composites for Construction Journal* 14(1): 36-48.
- Bianco, V., Monti, G., and Barros, J.A.O. (2014). "Design formula to evaluate the NSM FRP strips shear strength contribution to a RC beam." *Composites Part B: Engineering* 56: 960-971.
- Blanksvärd, T. (2009). Strengthening of concrete structures by the use of mineralbased composites. PhD Thesis, Luleå University of Technology.

- British Standards Institution (2001). Eurocode 2: Design of Concrete Structures: Part 1-1: General Rules and Rules for Buildings, British Standards Institution.
- Chaallal, O., Mofidi, A., Benmokrane, B., and Neale, K. (2011). "Embedded Through-Section FRP Rod Method for Shear Strengthening of RC Beams: Performance and Comparison with Existing Techniques." *Composites for Construction* 19: 374-383.
- Cisneros, D., Arteaga, A., De Diego, A., Alzate, A., and Perera, R. (2012). Experimental Study on NSM shear retrofiting of RC beams. 6th international conference on Composites in Civil Engineering, CICE 2012. Rome, Italy.
- Collins, M. P. (2001). Evaluation of shear design procedures for concrete structures. A Report prepared for the CSA technical committee on reinforced concrete design.
- De Lorenzis, L. and Nanni, A. (2001). "Shear Strengthening of Reinforced Concrete Beams with Near-Surface Mounted Fiber-Reinforced Polymer Rods." *ACI Structural Journal* 98: 60-68.
- Dias, S. J. E. (2008). Experimental and anlytical research in the shear strengthening of reinforced concreet beams using the near surface mounted technique with CFRP strips. PhD Thesis, University of Minho, Guimarães-Portugal, in Portugese.
- Dias, S. J. E., and Barros, J.A.O. (2011). "Shear strengthening of RC T-section beams with low concrete using NSM CFRP laminates." *Journal Cement & Concrete* Composites 3(2): 334-345.
- Dias, S. J. E. and Barros, J.A.O. (2008). "Shear Strengthening of T Cross Section Reinforced Concrete Beams by Near Surface Mounted Technique." *Journal of Composites for Construction*, ASCE 12(No.3): 300-311.
- Dias, S. J. E. and Barros, J.A.O. (2010). "Performance of reinforced concrete T beams strengthened in shear with NSM CFRP laminates." *Engineering Structures* 32: 373-384.
- Dias, S. J. E. and Barros, J.A.O. (2013). "Shear strengthening of RC beams with NSM CFRP laminates: Experimental research and analytical formulation." *Composite Structures* 99: 477-490.
- Gilman, J. R., Brickey, R.T., and Red, M.M. (1998). Monte Carlo Techniques for Evaluating Producing Properties, Society of Petroleum Engineers.
- Islam, A. A. (2009). "Effective methods of using CFRP bars in shear strengthening of concrete girders." *Engineering Structures* 31: 709-714.
- MathWorks, (2015). What Is Sensitivity Analysis?

- Moraes Neto, B., Barros, J., and Melo, G. (2014). "Model to Simulate the Contribution of Fiber Reinforcement for the Punching Resistance of RC Slabs." *Journal of Materials in Civil Engineering* 26(7).
- Rahal, K. N. (2010). "Near surface mounted shear strengthening of reinforced concrete beams." American Concrete Institute (ACI), Special Publication SP-272-13: 251-268.
- Rahal, K. N. and Rumaih, Hantem A. (2011). "Tests on reinforced concrete beams strengthened in shear using near surface mounted CFRP and steel bars." *Engineering Structures* 33: 53-62.
- Rizzo, A. and De Lorenzis, L. (2009). "Behaviour and capacity of RC beams strengthened in shear with NSM FRP reinforcement." *Construction and Building Materials* 3(No.4): 1555-1567.
- Saltelli et al. (2008). " Global Sensitivity Analysis ", John Wiley and Sons.
- Vecchio, F. J., Collins, M.P. (1986). "The Modified Compression-Field Theory for Reinforced Concrete Elements Subjected to Shear." *ACI Journal*: 219-231.

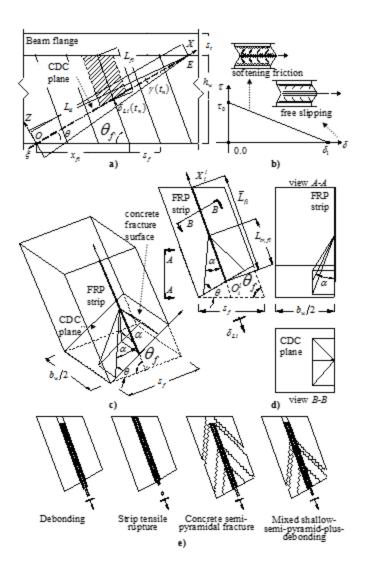


Fig. 1: Schematic representation of the Bianco *et al.* (2014) approach; a) average-available-bond-length NSM strip and concrete prism of influence; b) adopted local bond stress-slip relationship; c) NSM strip confined to the corresponding concrete prism of influence and semi-pyramidal fracture surface; d) sections of the concrete prism; e)

The mode of failure of an NSM FRP laminate subjected to an imposed end slip.

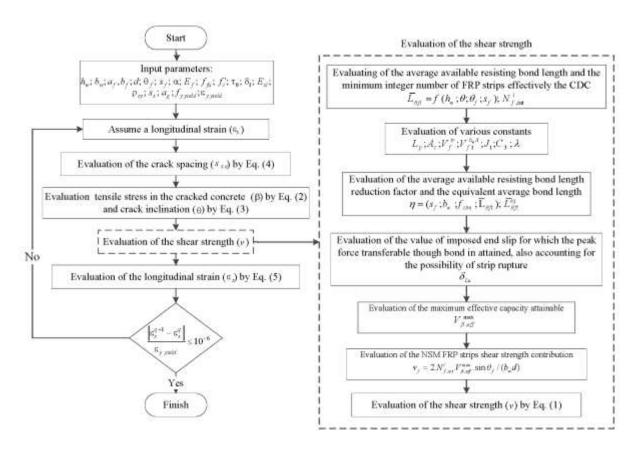


Fig. 2: Calculation procedure of BBB model

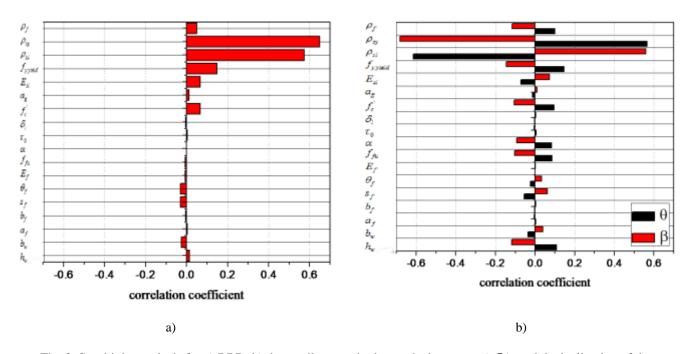


Fig. 3: Sensitivity analysis for a) BBB; b) the tensile stress in the cracked concrete (β); and the inclination of the diagonal compressive stress in the web of the section (θ)

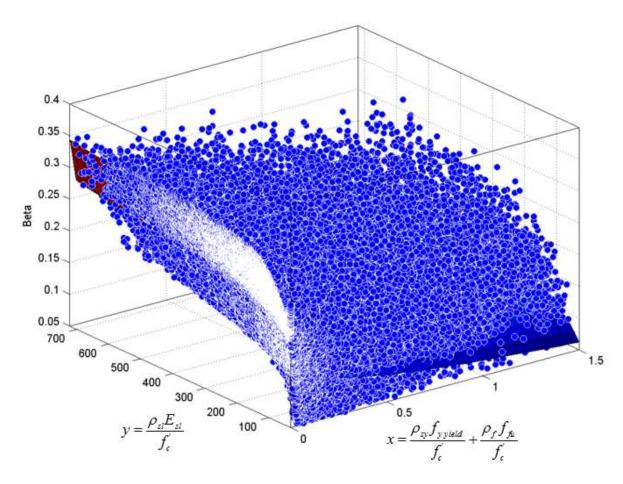


Fig. 4: Results of Monte Carlo simulation

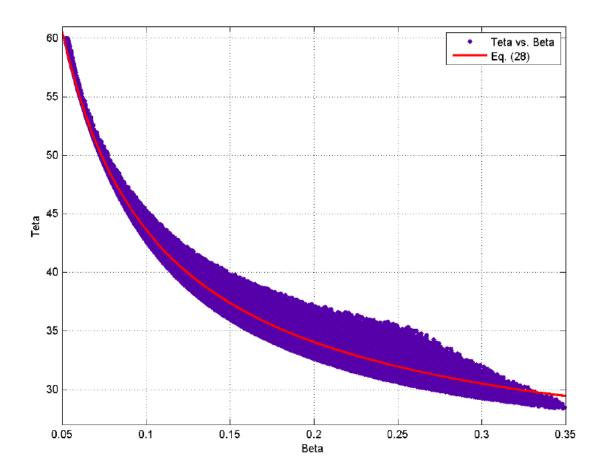
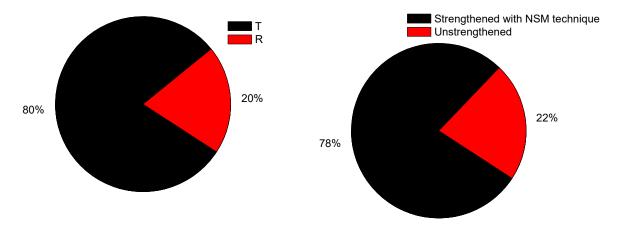
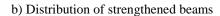
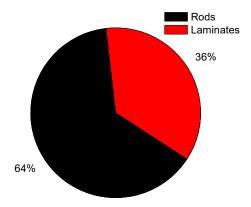


Fig. 5: Relation between θ_s and β_s (Eq. (28))



a) Distribution of rectangular and T cross section beams





c) Distribution of strengthened beams with FRP laminates and rods

Fig. 6: Characteristics of the database

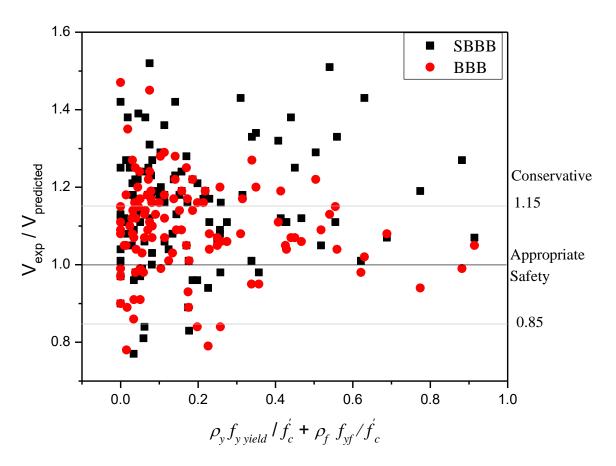


Fig. 7: Ratio between experimental and analytical model

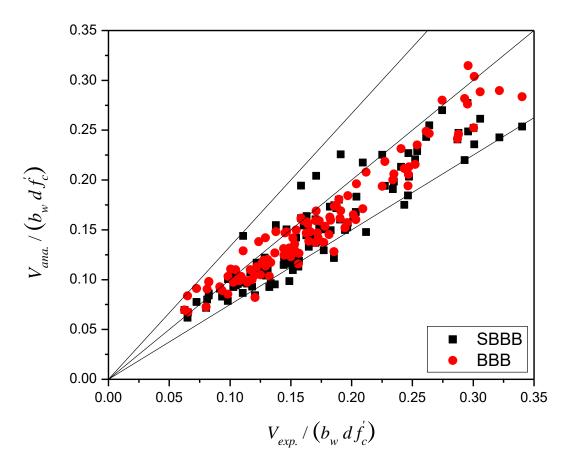


Fig. 8: Predicted non-dimensional shear failure force of the RC beams DB, in comparison with experimental values

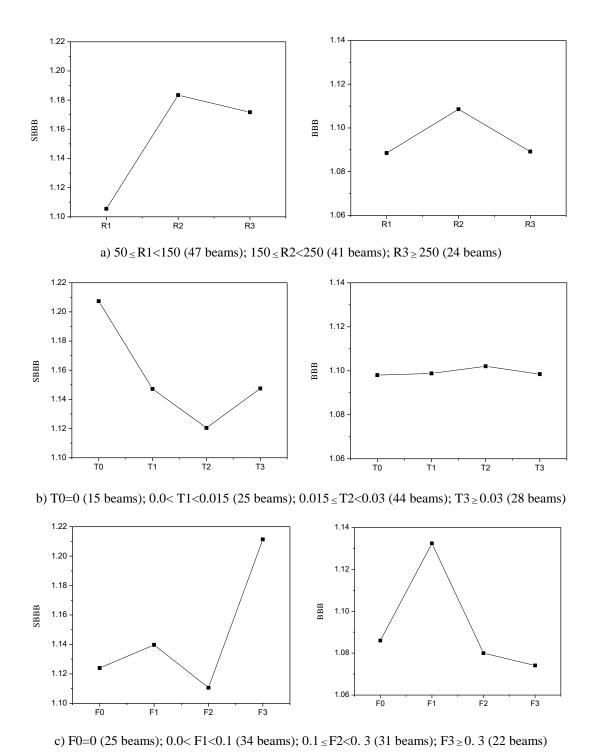


Fig. 9: Influence of the: a) R= $\rho_{sl}E_{sl}$ / $f_{c}^{'}$; b) T= $\rho_{sy}f_{yyield}$ / $f_{c}^{'}$; and c) F= $\rho_{f}f_{fu}$ / $f_{c}^{'}$ on the predictive performance of the models

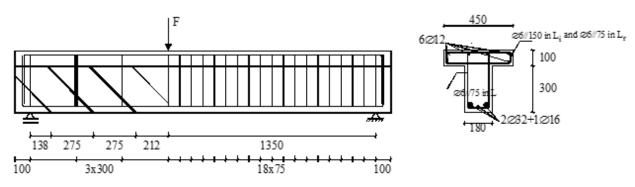


Fig. 10: geometry of the beam 2S-4LI45-I



Fig. 11: Crack inclination in 2S-4LI45-I beam

Table 1: Values characterizing the uniform probability distribution of the input parameters.

Table 2: Summary of experimental and analytical results applied to the DB

Table 3: Demerit points classification criteria

Table 4: Predictive performance of different approaches according to the modified version of the DPC

Table 5: Geometrical and mechanical data of the experimental RC beams

Table 6: BBB approach

Table 7: SBBB approach

Table 1: Values characterizing the uniform probability distribution of the input parameters.

	$h_{_{\!\scriptscriptstyle W}} \ mm$	$b_{_{\scriptscriptstyle W}} \ mm$	a_f mm	$b_f \ mm$	s_f mm	$ heta_f$ \circ	E_f GPa	$f_{\scriptscriptstyle fu} \ GPa$	α •	$ au_{0}$ MPa	$\delta_{_{1}}$ mm	f _c MPa	a _g mm	E_{sl} GPa	$f_{y yield}$ MPa	$ ho_{sl} \ (\%)$	ρ _{sy} (%)
Range of variation	200- 700	150- 400	1.0- 5.5	5- 35	50- 300	30- 90	100- 200	1.0-	10- 35	10- 30	2.0- 15. 0	15- 90	10- 40	180- 220	300- 700	1-4	0-

Table 2: Summary of experimental and analytical results applied to the DB

Beam Label	f _c (MPa)		Rei	inforcement		$V_{ m exp.}$ (kN)	$rac{V_{ ext{exp.}}}{V_{ extit{SBBB}}}$			
		$\frac{ ho_{sl}E_{sl}}{f_c^{'}}$	$ heta_f$	$\frac{ ho_{sy}f_{yyield}}{f_c^{'}}$	$\frac{ ho_f f_{fu}}{f_c'}$			$rac{V_{ m exp.}}{V_{ m \it BBB}}$		
			Dias a	and Barros (20	10; 2013)					
C-R-I			-	0	0	207	1.12	1.11		
2S-R-I			-	0.0143	0	304	1.27	1.18		
7S-R-I			-	0.038	0	467	1.22	1.25		
2S-4LV-I			90°	0.0143	0.056	337	1.18	1.09		
2S-7LV-I			90°	0.0143	0.09	374	1.20	0.99		
2S-10LV-I			90°	0.0143	0.12	397	1.08	1.03		
2S-4LI45-I		146.7	45°	0.0143	0.055	393	1.24	1.18		
2S-7LI45-I			45°	0.0143	0.09	422	1.07	1.05		
2S-10LI45-I			45°	0.0143	0.13	446	1.13	1.09		
2S-4LI60-I	39.7		60°	0.0143	0.049	386	1.29	1.22		
2S-6LI60-I			60°	0.0143	0.076	394	1.19	1.13		
2S-9LI60-I			60°	0.0143	0.11	413	1.04	1.01		
4S-R-II			-	0.0237	0	371	1.25	1.10		
4S-4LV-II			90°	0.0237	0.055	424	1.23	1.19		
4S-7LV-II			90°	0.0237	0.09	427	1.16	1.12		
4S-4LI45-II			45°	0.0237	0.055	442	1.18	1.17		
4S-7LI45-II			45°	0.0237	0.09	478	1.06	1.07		
4S-4LI60-II			60°	0.0237	0.048	444	1.25	1.22		
4S-6LI60-II			60°	0.0237	0.076	458	1.18	1.16		
Dias and Barros (2011)										
C-R-III	18.6	313.1	-	0	0	147	1.04	1.08		

2S-R-III			-	0.0304	0	226	1.09	1.08
4S-R-III			-	0.0508	0	304	1.14	1.17
2S-7LV-III			90°	0.0304	0.199	274	1.17	1.04
2S-4LI45-III			45°	0.0304	0.122	283	1.18	1.14
2S-7LI45-III			45°	0.0304	0.199	306	1.11	1.08
2S-4LI60-III			60°	0.0304	0.107	282	1.22	1.17
2S-6LI60-III			60°	0.0304	0.168	298	1.21	1.16
4S-7LV-III			90°	0.0508	0.199	315	1.07	1.05
4S-4LI45-III			45°	0.0508	0.122	347	1.16	1.17
4S-7LI45-III			45°	0.0508	0.199	356	1.06	1.07
4S-4LI60-III			60°	0.0508	0.107	346	1.19	1.19
4S-6LI60-III			60°	0.0508	0.168	362	1.19	1.19
			Dia	s and Barros	(2008)			
C-R-IV			-	0	0	243	1.42	1.47
2S-R-IV			-	0.0182	0	315	1.38	1.35
6S-R-IV			-	0.0303	0	410	1.21	1.27
2S-3LV-IV			90°	0.0182	0.057	316	1.31	1.24
2S-5LV-IV			90°	0.0182	0.095	357	1.36	1.29
2S-8LV-IV	24.4		90°	0.0182	0.152	396	1.28	1.25
2S-3LI45-IV	31.1	193.9	45°	0.0182	0.057	328	1.12	1.11
2S-5LI45-IV			45°	0.0182	0.095	384	1.18	1.18
2S-8LI45-IV			45°	0.0182	0.152	382	1.05	1.05
2S-3LI60-IV			60°	0.0182	0.057	374	1.52	1.45
2S-5LI60-IV			60°	0.0182	0.085	392	1.29	1.28
2S-7LI60-IV			60°	0.0182	0.123	406	1.23	1.22
			1	Dias (2008)			
C-R-V	59.4	108.6	T _ T	0	0	252	0.97	0.97

3S-R-V			_	0.0095	0	360	1.12	1.05
35 K V					Ü	300	1.12	
3S-6LV-V			90°	0.0095	0.025	387	0.96	0.91
3S-10LV-V			90°	0.0095	0.041	497	1.11	0.91
3S-5LI45-V			45°	0.0095	0.025	492	1.09	1.07
3S-9LI45-V			45°	0.0095	0.041	564	0.97	0.99
3S-5LI60-V			60°	0.0095	0.022	498	1.18	1.14
3S-8LI60-V			60°	0.0095	0.035	585	1.22	1.20
5S-R-VI			-	0.0143	0	410	1.11	1.05
5S-5LI45-VI			45°	0.0143	0.025	560	1.12	1.12
5S-9LI45-VI			45°	0.0143	0.041	627	0.99	1.03
5S-5LI60-VI			60°	0.0143	0.022	556	1.17	1.16
5S-8LI60-VI			60°	0.0143	0.035	655	1.24	1.24
			Cl	naallal <i>et al</i> . (2	2011)		l	1
S0-CON-I			-	0	0	122	1.01	0.99
S1-CON-I	25.0	304.0	-	0.0812	0	351	1.03	1.07
SO-NSM-I	20.0		90°	0	0.54	331	1.51	1.13
S1-NSM-I			90°	0.0812	0.54	356	1.01	0.98
S3-CON-II	35.0	217.1	-	0.0386	0	295	0.98	0.98
S3-NSM-II	22.0	217.1	90°	0.0386	0.39	306	1.11	1.04
		1	De Lor	enzis and Na	nni (2001)			
BV			-	0	0	181	1.13	1.09
B90-7			90°	0	0.31	230	1.43	1.08
B90-5	31.0	154.8	90°	0	0.44	255	1.38	1.07
B45-7			45°	0	0.45	331	1.25	1.07
B45-5			45°	0	0.63	356	1.43	1.02
BSV			-	0.029	0	306	1.05	1.12
BS90-7A			90°	0.029	0.31	414	1.33	1.27

			Rizzo	and De Loren	zis (2009)			
С			-	0.0401	0	244	1.12	1.04
NR90-73-b			90°	0.0401	0.5191	297	1.33	1.04
NR90-45-b			90°	0.0401	0.8421	305	1.27	0.99
NR45-146-a	29.3	317.3	45°	0.0401	0.3671	326	1.32	1.11
NR45-73-a			45°	0.0401	0.7341	300	1.19	0.94
NL90-73-a			90°	0.0401	0.3097	345	1.34	1.20
NL45-146-a			45°	0.0401	0.219	310	1.16	1.06
				Islam (2009	9)			
Beam1			-	0.0338	0	365	0.77	0.86
Beam2	49.75	68.3	90°	0.0338	0.1404	454	0.89	0.93
Beam3	47.13	00.5	90°	0.0169	0.1404	427	1.24	1.09
Beam4			90°	0.0008	0.1404	436	1.42	1.28
				Baghi (201	5)			
C-R-1		96.6	-	0	0	81	0.9	0.9
NSM-4L90-I		70.0	90°	0	0.082	143	1.20	1.1
C-R-II	32.7		-	0	0	214	1.25	1.15
7S-R-II		171.2	-	0.046	0	530	1.39	1.15
NSM-3L45-II			45°	0	0.064	291	1.38	1.14
		Rahal (2	2010) a	nd by Rahal a	and Rumaih	(2011)		
B1	37.6	125	-	0.017	0	300	1.08	1.02
B2-B90-R200	37.3	126	90°	0.017	0.045	410	1.06	1.07
B2-B90-F200	51.5	120	90°	0.017	0.169	440	1.22	1.14
B3-B90-R200A	37.8	124.3	90°	0.017	0.045	466	0.84	1.13
B3-B90-F200A	57.0	121.3	90°	0.017	0.169	510	0.96	1.22
B4-B45-R200	36.2	129.8	45°	0.017	0.064	526	1	1.16
B4-B45-F200	30.2	127.0	45°	0.017	0.240	576	1.08	1.2

B6-B45-R300	37.2	126.3	45°	0.017	0.042	380	0.81	0.98
B6-B45-F300	31.2	120.3	45°	0.017	0.160	410	0.83	1.01
		L	Ci	sneros et al. (2012)			
Control	27.97	150	-	0.015	0	113	1.05	0.78
B90-6a	26.69	157	90°	0.016	0.41	170	1.11	1.05
B90-6b	24.09	174	90°	0.017	0.45	163	1.12	1.06
B90-3a	22.84	183	90°	0.018	0.24	117	0.98	0.84
B90-3b	26.02	161	90°	0.016	0.21	117	0.94	0.79
B45-6a	22.98	182	45°	0.018	0.67	180	1.07	1.08
B45-6b	28.48	147	45°	0.015	0.54	212	1.11	1.15
B45-3a	29.11	144	45°	0.015	0.26	189	1.11	1.06
B45-3b	23.91	175	45°	0.018	0.32	155	1.01	0.95
S90-6a	26.69	157	90°	0.015	0.30	189	1.18	1.17
S90-6b	24.09	174	90°	0.017	0.34	147	0.98	0.95
S90-3a	22.84	183	90°	0.018	0.18	117	0.96	0.84
S90-3b	26.02	161	90°	0.016	0.16	131	1.01	0.89
S45-6a	22.98	182	45°	0.018	0.50	183	1.05	1.09
S45-6b	28.48	147	45°	0.014	0.40	221	1.12	1.19
S45-3a	29.11	144	45°	0.014	0.20	206	1.17	1.16
S45-3b	23.91	175	45°	0.017	0.24	173	1.09	1.06
		I	<u> </u>			Average	1.14	1.09
						SD	0.15	0.12
						COV	13.1%	11.0%
								1

Table 3: Demerit points classification criteria

$\lambda = V_{\text{exp.}} / V_{ana.}$	Classification	Penalty
<0.5	Extremely Dangerous	10
[0.5-0.85[Dangerous	5
[0.85-1.15[Appropriate Safety	0
[1.15-2[Conservative	1
≥2.0	Extremely Conservative	2

Table 4: Predictive performance of different approaches according to the modified version of the DPC

$\lambda = V_{\text{exp.}} / V_{ana.}$	SB	BB	BI	BB
exp. ana.	N° samples	Total	Nº samples	Total
<0.5	0	0	0	0
[0.5-0.85[4	20	4	20
[0.85-1.15[53	0	69	0
[1.15-2[55	55	39	39
≥ 2.0	0	0	0	0
\sum_{PEN}	112	75	112	59

Table 5: Geometrical and mechanical data of the experimental RC beams

Beam label	(mm)	h (mm)	h _w (mm)	d (mm)	a / d	f _c ' (MPa)	f _{l yield} (MPa)	$ ho_{sl}$ (%)	s (mm)	f _{y yield} (MPa)	ρ _{sy} (%)	$a_f \times b_f$ (mm ²)	D_f (mm)	$ heta_{\!\scriptscriptstyle f}$	s_f (mm)	E_f (GPa)	f_{fu} (MPa)	$\mathcal{E}_{\mathit{fiu}}$ (%)	V (kN)
	(11111)	(11111)	(11111)	(11111)		(IVII a)						(111111)	(111111)		(111111)	(Of a)	(MII a)	(70)	(== .)
							Dias	and Bar	ros (20	10; 2013))								
C-R-I									-	-	-								207
2S-R-I									300		0.105	-		-	-	-	-	-	304
7S-R-I									112.5		0.279								467
2S-4LV-I														90°	180				337
2S-7LV-I														90°	114				374
2S-10LV-I														90°	80				397
2S-4LI45-I														45°	275				393
2S-7LI45-I									300		0.105	13.3		45°	157	218.4	2863	1.33	422
2S-10LI45-I	180	400	300	360	2.5	39.7	759	2.8		542			-	45°	110				446
2S-4LI60-I														60°	243				386
2S-6LI60-I														60°	162				394
2S-9LI60-I														60°	108				413
4S-R-II														-	-	-	-	-	371
4S-4LV-II	_													90°	180				424
4S-7LV-II									180		0.175	13.3		90°	114	218.4	2863	1.33	427
4S-4LI45-II														45°	275				442
.5 12.15 11														15	2,3				1.2

Beam label	$b_{\scriptscriptstyle w}$	h	$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{\it sl}$	S	$f_{y yield}$	$ ho_{\scriptscriptstyle sy}$	$a_f \times b_f$	D_f	$\theta_{\scriptscriptstyle f}$	s_f	E_f	$f_{\it fu}$	${\cal E}_{\it fu}$	V
Beam raber	(mm)	(mm)	(mm)	(mm)	a / a	(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)	O_f	(mm)	(GPa)	(MPa)	(%)	(kN)
4S-7LI45-II														45°	157				478
4S-4LI60-II	1													60°	243				444
4S-6LI60-II	1													60°	162				458
			<u> </u>	<u> </u>				Dias and	Barros (2	2011)		l .	<u> </u>			l .			
C-R-III									-	-	-								147
2S-R-III	1								300		0.105	-		-	-	-	-	-	226
4S-R-III	1								180		0.174								304
2S-7LV-III	1													90°	114				274
2S-4LI45-III														45°	275				283
2S-7LI45-III									300		0.105			45°	157				306
2S-4LI60-III	180	400	300	360	2.5	18.6	734	2.8		539			-	60°	243				282
2S-6LI60-III										337		13.3		60°	162	174.3	2848	1.63	298
4S-7LV-III												10.0		90°	114	17.15	20.0	1.00	315
4S-4LI45-III	1													45°	275				347
4S-7LI45-III	1								180		0.174			45°	157				356
4S-4LI60-III	1													60°	243				346
4S-6LI60-III	1													60°	162				362
		1	ı	ı		1		Dias and	Barros (2	2008)	1	ı	ı	ı	1	1			
C-R-IV	180	400	300	356	2.5	31.1	444	2.9	-	-	-	-	-	-	-	-	-	-	243

Beam label	$b_{\scriptscriptstyle w}$	h	$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{\scriptscriptstyle sl}$	S	$f_{y \ yield}$	$ ho_{\scriptscriptstyle sy}$	$a_f \times b_f$	D_f	$ heta_{\scriptscriptstyle f}$	s_f	E_f	$f_{\it fu}$	${\cal E}_{\it fu}$	V
Beam laber	(mm)	(mm)	(mm)	(mm)	u / u	(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)	- 1	(mm)	(GPa)	(MPa)	(%)	(kN)
2S-R-IV									300		0.105								315
6S-R-IV									130		0.241								410
2S-3LV-IV														90°	267				316
2S-5LV-IV														90°	160				357
2S-8LV-IV														90°	100				396
2S-3LI45-IV										533				45°	367				328
2S-5LI45-IV									300		0.241	14		45°	220	166.6	2952	1.77	384
2S-8LI45-IV	_													45°	138				382
2S-3LI60-IV														60°	325				374
2S-5LI60-IV	_													60°	195				392
2S-7LI60-IV														60°	139				406
	1	I						Dia	s (2008)					l					
C-R-V									-	-	-	-		_				_	252
3S-R-V	_																		360
3S-6LV-V														90°	180				387
3S-10LV-V	180	400	300	360	3.33	59.4	716	3.1	300	551	0.105	13.3	-	90°	114				497
3S-5LI45-V									300	331	0.105	13.3		45°	275	174.3	2848	16.3	492
3S-9LI45-V														45°	157				564
3S-5LI60-V														60°	243				498

Beam label	$b_{\scriptscriptstyle w}$	h	$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{sl}$	S	$f_{y yield}$	$ ho_{sy}$	$a_f \times b_f$	D_f	$\theta_{\scriptscriptstyle f}$	s_f	E_f	$f_{\it fu}$	${\cal E}_{\it fu}$	V
Beam laber	(mm)	(mm)	(mm)	(mm)	u / u	(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)	0,1	(mm)	(GPa)	(MPa)	(%)	(kN)
3S-8LI60-V														60°	162				585
5S-R-VI												-		-	-	-	-	-	410
5S-5LI45-VI														45°	275				560
5S-9LI45-VI									200		0.157	13.3		45°	157	174.3	2848	16.3	627
5S-5LI60-VI												13.3		60°	243	174.3	2040	10.5	556
5S-8LI60-VI	-													60°	162				655
	1							Chaallal	et al. (20	011)				l		l			
S0-CON-I									-	-	-		_	_	_	_	_	_	122
S1-CON-I	_					25	470		175	540	0.376		-	-	_	-	-	-	351
SO-NSM-I	152	406	304	350	2	23	470	3.7	-	-	-		9.5	90°	130	148	1885	1.27	331
S1-NSM-I	132	400	304	330	3			5.7	175	540	0.376	-	9.3	90	130	140	1003	1.27	356
S3-CON-II						35	(50)		262.5	650	0.251		-	-	-	-	-	-	295
S3-NSM-II						33	650		262.5	650	0.251		9.5	90°	130	148	1885	1.27	306
	1						De	Lorenzis	and Nan	ni (2001)									<u> </u>
BV													-	-	-	-	-	-	181
B90-7	1													90°	178				230
B90-5	152	406	304	356	3	31	414	2.4	-	-	-	-	0.7	90°	127	1040	1077	1.50	255
B45-7	-												9.5	45°	178	104.8	1875	1.79	331
B45-5	1													45°	127				356

Beam label	$b_{_{\scriptscriptstyle W}}$	h	$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{sl}$	S	$f_{y yield}$	$ ho_{\scriptscriptstyle sy}$	$a_f \times b_f$	D_f	$ heta_{\!\scriptscriptstyle f}$	s_f	E_f	$f_{\it fu}$	${\cal E}_{fu}$	V
	(mm)	(mm)	(mm)	(mm)		(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)		(mm)	(GPa)	(MPa)	(%)	(kN)
BSV									356	345	0.291		-	-	-	-	-	-	306
BS90-7A									330	343	0.291		9.5	90°	178	104.8	1875	1.79	414
							Riz	zo and Do	e Lorenzi	is (2009)									
С												_	-	-	-	-	-	-	244
NR90-73-b														90°	73				297
NR90-45-b												_	8	90°	45	145.7	2214	1.52	305
NR45-146-a	200	210	210	173	3	29.3	544	4.4	160	665.3	0.177			45°	146				326
NR45-73-a														45°	73				300
NL90-73-a														90°	73				345
												32				121.5	2068	1.7	
NL45-146-a														45°	146				310
								Islaı	n (2009)										
Beam1									152		0.34		-	-	-	-	-	-	365
Beam2									152		0.34			90°	152				454
Веат3	254	305	305	261	2.34	49.75	414	1.7	305	414	0.168	-	9	90°	305	124	2068	1.66	427
													7			124	2008	1.00	
Beam4									610		0.085			90°	152				436
	1		1	ı	1	l		Bagl	ni (2015))	ı		ı		1	1			1
C-R-1												-		-	-	-	-	-	81
NSM-4L90-I	150	300	300	264	3	32.7	580	1.6	-	-	-	14	_	90°	180	150	2620	1.6	143
	100	400	200	260	2.5		605	20											
C-R-II	180	400	300	360	2.5		625	2.8	-	-	-	-		-	-	-	-	-	214

		$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{\scriptscriptstyle sl}$	S	$f_{y \ yield}$	$ ho_{\scriptscriptstyle sy}$	$a_f \times b_f$	D_f	$ heta_{\scriptscriptstyle f}$	\mathbf{s}_f	E_f	$f_{\it fu}$	$\mathcal{E}_{\mathit{fu}}$	V
mm)	(mm)	(mm)	(mm)		(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)		(mm)	(GPa)	(MPa)	(%)	(kN)
								112.5	500	0.279			-	-				530
								-	-	-	14		45°	275	150	2620	1.6	291
					Ra	hal (2010) and by	Rahal an	d Rumaih	(2011)								
					37.6							-	-	-	-	-	-	300
													90°	200	210	510	0.24	410
					37.3								90°	200	124	1900	1.53	440
								200		0.188			90°	200	210	510	0.24	466
150	500	400	430	3	37.8	446	2.35		338		-		90°	200	124	1900	1.53	510
												8	45°	200	210	510	0.24	526
					36.2								45°	200	124	1900	1.53	576
													45°	300	210	510	0.24	380
					37.2			300		0.126			45°	300	124	1900	1.53	410
							Cisneros	et al. (2)	012)									
1				L	27.07	- 1	Cisileros	- Cr an. (2	012)	ı		ı			ı		ı	112
												-			-	-	-	113
					26.69								90°	115				170
					24.09								90°	115				163
200	350	350	310	3	22.84	446	2.0	230	338	0.123	-	8	90°	230	165	2500	1.51	117
					26.02								90°	230				117
					22.98								45°	115				180
	50					37.6 37.3 37.8 37.8 36.2 37.2 37.2 37.2 37.2	37.6 37.3 37.8 37.8 36.2 37.2 37.2 37.2 37.2 37.2 37.2	37.6 37.3 37.8 446 2.35 36.2 37.2 Cisneros 27.97 26.69 24.09 24.09 24.09 24.09 24.09 24.09 24.09 24.09 24.09 24.09 24.09 24.09 26.02	Rahal (2010) and by Rahal an 37.6	Rahal (2010) and by Rahal and Rumaih 37.6 37.3 37.8 446 2.35 338 Cisneros et al. (2012) 27.97 26.69 24.09 24.09 22.84 26.02	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Rahal (2010) and by Rahal and Rumaih (2011) 37.6	Solution Solution

Beam label	$b_{_{\scriptscriptstyle W}}$	h	$h_{_{\scriptscriptstyle W}}$	d	a / d	$f_c^{'}$	$f_{l \ yield}$	$ ho_{\scriptscriptstyle sl}$	S	$f_{y \ yield}$	$ ho_{\scriptscriptstyle sy}$	$a_f \times b_f$	D_f	$ heta_{\scriptscriptstyle f}$	S_f	E_f	$f_{\it fu}$	$\mathcal{E}_{\mathit{fu}}$	V
Beam facer	(mm)	(mm)	(mm)	(mm)	a / a	(MPa)	(MPa)	(%)	(mm)	(MPa)	(%)	(mm ²)	(mm)	J	(mm)	(GPa)	(MPa)	(%)	(kN)
B45-6b						28.48								45°	115				212
B45-3a						29.11								45°	230				189
B45-3b						23.91								45°	230				155
S90-6a						26.69								90°	115				189
S90-6b						24.09								90°	115				147
S90-3a	•					22.84								90°	230				117
S90-3b						26.02						37.5	_	90°	230				131
S45-6a						22.98								45°	115				183
S45-6b						28.48								45°	115				221
S45-3a						29.11								45°	230				206
S45-3b						23.91								45°	230				173

2 3

Table 6: BBB approach										
Iteration	$A = \varepsilon_x$ Estimated	S_{xe}	β	θ	v_c	v_s	v_f	v	$B = \varepsilon_{x}$ $Eq. (5)$	A- B
1	0.001	276.58	0.1629	35.66	1.03	0.79	0.84	2.66	4.55e-4	5.45e-4
2	5.11e-4	276.58	0.2307	32.27	1.45	0.90	0.95	3.30	7.43e-4	-2.32e-4
3	7.43e-4	276.58	0.1926	33.88	1.21	0.84	0.90	2.95	6.17e-4	1.26e-4
4	6.17e-4	276.58	0.2115	33.01	1.33	0.87	0.93	3.13	6.81e-4	-6.40e-5
5	6.81e-4	276.58	0.2015	33.45	1.27	0.86	0.91	3.04	6.48e-4	3.30e-5
6	6.48e-4	276.58	0.2066	33.22	1.30	0.87	0.92	3.09	6.65e-4	-1.70e-5
7	6.65e-4	276.58	0.2039	33.34	1.28	0.86	0.91	3.06	6.55e-4	1.00e-5
8	6.55e-4	276.58	0.2053	33.28	1.29	0.86	0.92	3.07	6.61e-4	-6.00e-6
9	6.61e-4	276.58	0.2046	33.31	1.29	0.86	0.92	3.07	6.61e-4	0

Table 7: SBBB approach

Iteration	$x = \frac{\rho_{sy} f_{yyield}}{f_c^{\cdot}} + \frac{\rho_f f_{fu}}{f_c^{\cdot}}$	$y = \frac{\rho_{sl} E_{sl}}{f_c'}$	$oldsymbol{eta}_s$	$ heta_{s}$	ν				
1	0.0693	146.7	0.195	34.35	2.93				