# STRESS-STRAIN MODEL FOR PARTIAL CFRP CONFINED CONCRETE

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**Keywords:** Carbon Fiber Reinforced Polymers, Confinement, Concrete, Columns, Confinement model.

Summary: Concrete columns requiring strengthening intervention always contain a certain percentage of steel hoops. Applying strips of wet lay-up carbon fiber reinforced polymer (CFRP) sheets in-between the existent steel hoops might, therefore, be an appropriate confinement technique with both technical and economic advantages, when full wrapping of a concrete column is taken as a basis of comparison.

To assess the effectiveness of the partial wrapping technique, circular cross section concrete columns were confined by distinct CFRP arrangements and tested under direct compression. The experimental program was designed to evaluate the influence of the concrete strength class, the stiffness of the wet lay-up CFRP sheet, the distance between strips, the width of the strip, and the number of layers per each strip.

The Harajli et al. model was modified in order to predict the compression stress-strain behaviour of reinforced concrete column elements partially and totally confined by CFRP lay-up sheets. The main results of the experimental program are hereby presented and analysed. The model's performance is assessed using the experimental results.

## **1 INTRODUCTION**

Reinforcement concrete columns can be strengthened by a carbon fiber reinforced polymer (CFRP) jacket, which provides lateral confinement to the column. Applying strips of wet lay-up CFRP sheets inbetween the existing steel hoops might, therefore, be an appropriate confinement technique with both technical and economic advantages, when full wrapping of a concrete column is taken as a basis of comparison.

Analytical models have been proposed to simulate the stress-strain compression response of full FRPwrapped concrete elements [1-5]. The applicability of these models to predict the behaviour of concrete columns confined by discrete CFRP arrangements is still limited.

In the present work, the principles proposed by Harajli *et al.*, were used to develop a confinement model to simulate, not only full wrapped specimens but also those with discrete arrangements. The performance of the model was appraised using results obtained in the experimental program carried out.

#### 2 EXPERIMENTAL PROGRAM AND CONFINEMENT ARRANGEMENTS

The experimental program deals with direct compression tests with reinforced concrete (RC) column elements of 600 mm high and 200 mm diameter. This program is composed by several groups of tests in order to evaluate the influence of the following parameters on the load carrying and deformation capacity of RC elements submitted, predominantly, to compression loading: concrete strength class (two compressive strengths, 16MPa and 32MPa ,were selected); stiffness of the CFRP-based confinement system (two CFRP sheets were used, one of 300 g/m<sup>2</sup> of fibers and the other of 200 g/m<sup>2</sup> of fibers); width (W) and spacing (s') of the CFRP strips; number of CFRP layers per strip (L); percentage of the longitudinal,  $\rho_{sl}$ , and transversal,

 $\rho_{st}$ , steel reinforcement ratio. Due to lack of space, only the groups of tests C16S200 $\Phi$ 8, C16S300 $\Phi$ 8, C32S200 $\Phi$ 8 and C32S300 $\Phi$ 8, indicated in Table 1, are analyzed in the present paper.



Table1 – Experimental program

The confinement systems are composed by strips of CFRP sheet bonded to concrete and to subjacent layers by epoxy resin. Each specimen is designated by  $W_iS_jLk$ , where  $W_i$  is the strip width,  $S_j$  is the number of strips along the specimen and Lk is the number of CFRP layers per each strip. In the adopted designation for a group of test series, the C16 and C32 designation indicates that concrete specimens with an average compressive strength of 16 and 32 MPa, respectively, while S200 and S300 denote the type of CFRP sheet, 200 g/m<sup>2</sup> and 300 g/m<sup>2</sup>, respectively. Finally,  $\Phi$ 8 indicates the diameter, in mm, of the longitudinal steel bars.

As Figure 1 shows, the partially-wrapped specimens are confined by six strips (W45S6 and W60S6). These three test series have two sub-series, one of three layers per strip (L3) and another with five layers per strip (L5).







W600S1

Figure 1 : Confinement arrangements

## **3 EXPERIMENTAL RESULTS**

Tables 2 and 3 include the main effectiveness indicators provided by the applied confinement systems. In these tables,  $f_{co,UPC}$  is the compressive strength of unconfined plain concrete specimens (UPC),  $f_{co,URC}$  is the compressive strength of unconfined reinforced concrete specimens,  $\varepsilon_{co,UPC}$  is the specimen axial strain corresponding to  $f_{co,UPC}$  and  $\varepsilon_{co,UPC}$  is the specimen axial strain corresponding to  $f_{co,UPC}$  and  $\varepsilon_{co,UPC}$  is the specimen axial strain corresponding to  $f_{co,UPC}$ . Each value in Tables 2 and 3 is the average of results obtained in the two specimens of each series. In specimens W600S1L5 of C32S200 $\phi$ 8 and in specimens W60S6L5, W600S1L3 and W600S1L5 of C32S300 $\phi$ 8 series (fully wrapped specimens) the maximum load carrying capacity of the equipment was attained without failure of these specimens. The values indicated in Table 3 correspond to the end of this test phase. Since the load carrying capacity of the equipment can be doubled if the tests are carried out in a non-closed loop control, the specimens of these series were again tested up to their failure, and the attained  $f_{cc}$  values are indicated in Table 3 within square brackets. As it was impossible to record strains in the CFRP during this second loading phase of these tests, only the compressive strength was recorded.

Results of Table 2 indicate that, in C16S200 $\phi$ 8,  $f_{co,URC}$  varied from 1.9 in series confined with strips of 45 mm width and three layers per strip (W45S5L3),  $\rho_{=}0.31\%$ , up to 4.2 in the fully-wrapped series with five layers,  $\rho_{=}1.13\%$ . For C16S300 $\phi$ 8 these limit values increased to 2.5 and 5.1, respectively, since the CFRP confinement ratio increased due to the higher thickness of the CF130 sheet (from  $\rho_{=}0.48\%$  up to  $\rho_{=}1.76\%$ ). Table 3 shows that, in the case of C32S200 $\phi$ 8,  $f_{co}/f_{co,URC}$  varied from 1.37 for  $\rho_{=}0.48\%$  up to 2.99 for  $\rho_{=}1.13\%$ , while for C32S300 $\phi$ 8 the values were in the range 1.60 to 3.27 for  $\rho_{=}0.48\%$  and  $\rho_{f}$  =1.76%, respectively. In terms of  $\varepsilon_{co}/\varepsilon_{co,URC}$ , the values ranged from 4.8 up to 10.5 for C16S200 $\phi$ 8 series, 7.3 up to 14.8 for C16S300 $\phi$ 8, 3.1 up to 6.1 for C32S200 $\phi$ 8 and 4.0 up to 7.5 for C32S300 $\phi$ 8. However, the upper bound values of the ranges of  $\varepsilon_{co}/\varepsilon_{co,URC}$  for these last two series of tests would have been greater if the strains in the CFRP of the specimens, that have not failed in the closed loop control test phase, had been recorded in the non-closed loop control phase. In all series of tests, the increase of  $\varepsilon_{co}/\varepsilon_{co,URC}$  ratio with  $\rho_{f}$  was more pronounced in specimens of discrete confinement arrangements than in fully-wrapped specimens. The plastic deformation of the concrete in-between the CFRP strips may justify this occurrence.

The last column of Tables 2 and 3 shows that, at specimen failure always occurring by the CFRP tensile rupture, the maximum tensile strain in the direction of the fibers,  $\varepsilon_{imax}$ , varied from 27% up to 88% of the CFRP ultimate tensile strain,  $\varepsilon_{iu}$ . These values are only for specimens that failed when the equipment was working in closed-loop control. As Lam and Teng (2003) have already reported, the variation of the strain field in the CFRP depends considerably on the distribution of the damage in the concrete specimen. Taking this into account and considering that only one or two strain gauges were applied per specimen for recording the CFRP strain variation, it is not surprising that a tendency was not determined for the  $\varepsilon_{imax}/\varepsilon_{fu}$  ratio. A high scatter was registered on the maximum strain values in the CFRP, since the recorded values only represent the areas where the strain gauges were placed. Hence, these values are too dependent on the specimen failure mode configuration.

Image         Image <th< th=""><th>Type of sheet</th><th>Specimen designation</th><th>L</th><th><math>\binom{\rho_f}{(\%)}</math></th><th>f<sub>cc</sub> (MPa)</th><th><math>\binom{\mathcal{E}_{cc}}{(\%)}</math></th><th>f<sub>cc</sub>/f<sub>co,URC</sub></th><th><math>\mathcal{E}_{cc}/\mathcal{E}_{co,URC}</math></th><th><math>\mathcal{E}_{fmax}</math> (%)</th><th><math>\mathcal{E}_{fmax}/\mathcal{E}_{fu}</math></th></th<>	Type of sheet	Specimen designation	L	$\binom{\rho_f}{(\%)}$	f <sub>cc</sub> (MPa)	$\binom{\mathcal{E}_{cc}}{(\%)}$	f <sub>cc</sub> /f <sub>co,URC</sub>	$\mathcal{E}_{cc}/\mathcal{E}_{co,URC}$	$\mathcal{E}_{fmax}$ (%)	$\mathcal{E}_{fmax}/\mathcal{E}_{fu}$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		Unconf. plain concrete (UPC)			13.87 (f <sub>co.UBC</sub> )	0.003	-	-	-	-
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		Unconf. Reinf. Conc. (URC)			$(f_{co,UPC})$	0.004 $(\varepsilon_{co,UPC})$	-	-	-	-
C16S20048         W45S6L3         3         3         27.68         0.019         1.88         4.75         (SG1)         (SG1)         (SG1)         (SG2)         (SG					( 00,0/10/	1 00,01107			0.0069	0.44
C16S20008         W45S6L3         3         0.48         36.04         0.034         2.45         7.25         0.0083         0.53           C16S30008         0.48         36.04         0.034         2.45         7.25         0.0084         0.55           C16S20008         0.48         36.04         0.034         2.45         7.25         0.0084         0.55           C16S20008         0.48         35.50         0.030         2.41         7.50         0.0089         0.57           C16S30008         0.48         35.50         0.030         2.41         7.50         0.0089         0.57           C16S30008         0.80         45.82         0.047         3.11         11.75         0.00934         0.60           C16S20008         0.605         0.80         45.82         0.047         3.11         11.75         0.0073         0.47           C16S20008         0.604         45.82         0.047         3.11         11.75         0.0078         0.51           C16S20008         0.604         45.83         0.037         3.14         0.0078         0.51           C16S20008         0.605         0.68         43.53         0.035         2.96	0.400000.00			0.31	27.68	0.019	1 88	4.75	(SG1)	(SG1)
W45S6L3         3	C16S200ø8				27.00	0.019	1.00		0.0083	0.53
C16S300\0000000000000000000000000000000000									(SG2)	(SG2)
C16S300068		W45S6L3	3						0.00846	0.55
$ \begin{array}{c} \label{eq:classe} \begin{tabular}{ c c c c c c c } \hline C16S200 \phi 8 \\ \hline C16S200 \phi 8 \\ \hline C16S200 \phi 8 \\ \hline C16S300 \phi 8 \end{array} \\ \hline W45S6L5 \\ \hline C16S300 \phi 8 \\ \hline W60S6L3 \\ \hline C16S200 \phi 8 \\ \hline W60S6L3 \\ \hline C16S200 \phi 8 \\ \hline W60S6L5 \\ \hline C16S200 \phi 8 \\ \hline C16S200 \phi 8 \\ \hline W60S6L5 \\ \hline C16S200 \phi 8 \\ \hline C16S200 \phi 8 \\ \hline W60S6L5 \\ \hline C16S200 \phi 8 \\ \hline U17 \\ \hline U17$	040000010			0.48	36.04	0.034	2.45	7.25	(SG1)	(SG1)
C16S200068         Image: Here Here Here Here Here Here Here He	C16S300ø8								0.0103	0.65
C16S200\0000000000000000000000000000000000									(SG2)	(SG2)
C16S200008         W45S6L5         5         0.51         35.50         0.030         2.41         7.50         (SG1)         (SG4)           C16S300008         W45S6L5         5         0.80         45.82         0.047         3.11         11.75         0.0034         0.60           C16S200008         0.80         45.82         0.047         3.11         11.75         0.0034         0.60           C16S200008         0.61         34.36         0.022         2.34         5.50         0.0078         0.51           C16S200008         0.64         46.13         0.022         2.34         5.50         0.0078         0.51           C16S300008         0.64         46.13         0.037         3.14         9.25         (SG1)         (SG1)           C16S200008         0.64         46.13         0.037         3.14         9.25         (SG1)         (SG1)           C16S200008         0.68         43.53         0.035         2.96         8.75         (SG1)         (SG1)           C16S300008         1.06         64.96         0.059         4.42         14.75         (SG1)         (SG1)           C16S300008         1.06         64.96         0.059					35 50	0.030	2.41	7.50	0.0089	0.57
C16S20008         W45S6L5         5         6         6000         <	040000040			0.51					(SG1)	(SG1)
W45S6L5         6         7 </td <td>C165200ø8</td> <td></td> <td></td> <td></td> <td>00.00</td> <td>0.0073</td> <td>0.47</td>	C165200ø8				00.00				0.0073	0.47
C16S300008         W4350L3         5         6         45.82         0.047         3.11         11.75         0.00934         0.60           C16S300008         - <td< td=""><td></td><td></td><td>Б</td><td></td><td></td><td>(SG2)</td><td>(SG2)</td></td<>			Б						(SG2)	(SG2)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		W4556L5	Э						0.00934	0.60
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	C16S20049			0.80	45.82	0.047	3.11	11.75	(SG1)	(SG1)
C16S200\overline{8}         W60S6L3         0.41         34.36         0.022         2.34         (SG2)         (SG2)         (SG1)         (SG1)         (SG1)         (SG1)         (SG1)         (SG2)         (SG2)         (SG1)         (SG1)         (SG2)         (SG2)         (SG1)         (SG1)         (SG1)         (SG1)         (SG2)         (SG1)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG1)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)         (SG2) <td>C 16530008</td> <td></td> <td></td> <td></td> <td>10102</td> <td>0.011</td> <td>0.11</td> <td></td> <td>0.00828</td> <td>0.53</td>	C 16530008				10102	0.011	0.11		0.00828	0.53
C16S200\overline{B}         W60S6L3         4         34.36         0.022         2.34         5.50         0.0078         0.51           C16S300\overline{B}         W60S6L3         3         4         0.022         2.34         5.50         0.0078         0.022         (SG1)         0.0066         0.42           C16S300\overline{B}         0.64         46.13         0.037         3.14         9.25         0.0126         0.82           C16S200\overline{B}         0.64         46.13         0.037         3.14         9.25         0.0126         0.82           C16S200\overline{B}         0.64         43.53         0.035         2.96         8.75         0.0092         0.59           C16S300\overline{B}         0.685         43.53         0.059         4.42         14.75         0.0137         0.88           C16S300\overline{B}         1.06         64.96         0.059         4.42         14.75         0.0137         0.88           C16S300\overline{B}         1.06         64.96         0.059         4.42         14.75         0.0137         0.88           (SG1)         (SG1)         (SG1)         (SG1)         (SG1)         0.79           (SG2)         (SG2)									(SG2)	(SG2)
C16S200068         W60S6L3         3         0.41         34.36         0.022         2.34         5.50         (SG1)         (SG1)           C16S300068         W60S6L3         3         -	C16S200ø8		3	0.41	34.36	0.022	2.34	5.50	0.0078	0.51
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									(SG1)	(SG1)
W60S6L3         3         Image: Head Head Head Head Head Head Head Head		W60S6L3							0.0066	0.42
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									(SG2)	(SG2)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	0.400000.00				46.13	0.037	3.14	9.25	0.0126	0.82
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				0.64					(SG1)	(SG1)
С16S200ф8         W60S6L5         5         0.68         43.53         0.035         2.96         8.75         0.0092         0.59           C16S300ф8         W60S6L5         5         43.63         0.035         2.96         8.75         0.0092         0.59           C16S300ф8         1.06         64.96         0.059         4.42         14.75         0.0137         0.88           (SG1)         (SG1)         (SG1)         (SG1)         (SG1)         0.0122         0.79           (SG2)         (SG2)         (SG2)         (SG2)         0.59         0.0122         0.79	C16S300ø8								0.0120	0.78
$\begin{array}{c} \begin{array}{c} \\ C16S200\phi8 \\ C16S300\phi8 \end{array} \\ \end{array} \\ \begin{array}{c} W60S6L5 \end{array} \\ \begin{array}{c} \\ C16S300\phi8 \end{array} \\ \end{array} \\ \begin{array}{c} \\ W60S6L5 \end{array} \\ \begin{array}{c} \\ \\ \\ \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \\ \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \\ \end{array} \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \begin{array}{c} \\ \\ \end{array} \\ \end{array} \\ \begin{array}{c} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \\ \end{array} \\ \begin{array}{c} \\ \end{array} \\ $									(SG2)	(SG2)
С16S200ф8         W60S6L5         5         0.68         43.53         0.035         2.96         8.75         (SG1)         (SG2)           C16S300ф8         W60S6L5         5         -	C16S200ø8	W60S6L5	5	0.68	43.53	0.035	2.96	8.75	0.0092	0.59
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									(SG1)	(SG1)
W60S6L5         5									0.0060	0.44
C16S300\phi8 \ \ C16S300\phi8 \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \									(SG2)	(SG2)
C16S300\phi8         1.06         64.96         0.059         4.42         14.75         (SG1)         (SG1)           0.0122         0.79         (SG2)         (SG2)         (SG2)         (SG2)         (SG2)	C16S300ø8			1.06	64.96		4.42	14.75	0.0137	0.88
(SG2) (SG2)						0.059			(SG1)	(SG1)
(SG2) (SG2)									0.0122	0.79
									(SG2)	(SG2)
				0.68	47.02	0 022	2.06	Ø 00	0.0098	0.63
C16S200\u00f68   C16S200  C	C16S200ø8			0.00	47.95	0.032	3.20	0.00	(SG1)	(SG1)
W600S1L3 3 4 00 00769 0.50		W600S1L3	3	4.00					0.00769	0.50
$C16S300\phi8$ $1.06$ $52.19$ $0.033$ $3.55$ $8.25$ $(SG1)$ $(SG1)$	C16S300ø8			1.06	52.19	0.033	3.55	8.25	(SG1)	(SG1)
	C16S200+9			1.13	61.98	0.042	4.21	10.5	0.010	0.65
(SG1) (SG1)	C 10320048	M0000041 5	_		0.100				(SG1)	(SG1)
VV600S1L5 5 0.470 75.40 0.050 5.44 40.50 0.00757 0.49	040000010	W600S1L5	5	4 70	75.40	0.050	<b>F</b> 44	40.50	0.00757	0.49
C1053000φ8   1.76 75.18 0.050 5.11 12.50 (SG1) (SG1)	C16530068			1.76	75.18	0.050	5.11	12.50	(SG1)	(SG1)

Table 2. Main indicators of the efficacy of the confinement systems in the  $C16S200\phi 8$  and  $C16S300\phi 8$  test series.

Type of sheet	Specimen designation	L	$\binom{\rho_f}{(\%)}$	f <sub>cc</sub> (MPa)	$\binom{\mathcal{E}_{cc}}{(\%)}$	f <sub>co</sub> /f <sub>co,URC</sub>	$\varepsilon_{cc}/\varepsilon_{co,URC}$	E <sub>fmax</sub> (%)	$\mathcal{E}_{fmax}/\mathcal{E}_{fu}$
	Unconf. plain concrete (UPC)			30.31 (f <sub>co,UPC</sub> )	0.003 (ε <sub>co,UPC</sub> )	-	-	-	-
	Unconf. Reinf. Conc. (URC)			32.80 (f <sub>co UBC</sub> )	0.003 (ε <sub>co UBC</sub> )	-	-	-	-
			0.01	44.90	0.0000	4.07	2.07	0.00867 (SG1)	0.56 (SG1)
C32S200ø8			0.51	44.00	0.0092	1.57	5.07	0.00422 (SG2)	0.27 (SG2)
000000000	W45S6L3	3	0.48	52.76	0.0132	1.60	4.40	0.00743 (SG1)	0.47 (SG1)
C32S300ø8			0.40		0.0132			0.00585 (SG2)	0.38 (SG2)
			0.54	55.00	0.0400	4.00	4.60	0.00702 (SG1)	0.45 (SG1)
C32S200ø8			0.51	55.50	0.0139	1.09	4.03	0.00672 (SG2)	0.43 (SG2)
	W45S6L5	5	0.80	60.70	0.0185	1.85	6.17	0.00883 (SG1)	0.57 (SG1)
C32S300ø8								0.00796 (SG2)	0.51 (SG2)
<b>.</b>			0.44	54.07	0.0407	4.00	4 57	0.00731 (SG1)	0.47 (SG1)
C32S200ø8			0.41	54.57	0.0137	1.00	4.37	0.00822 (SG2)	0.53 (SG2)
	W60S6L3	3	0.62	62 50	0.0495	1.94	6.17	0.00689 (SG3)	0.44 (SG1)
C32S300ø8			0.03	63.50	0.0185			0.00711 (SG4)	0.46 (SG2)
				07.00	0.0470	0.05	5.07	0.00721 (SG1)	0.47 (SG1)
C32S200ø8			0.68	67.09	0.0179	2.05	5.97	0.00804 (SG2)	0.52 (SG2)
C32S300ø8	W60S6L5	5	1.06	71.52* 84.44**	0.0225	2.18* 2.57**	7.50	0.00902 (SG1)	0.58 (SG1)
								0.00764 (SG2)	0.49 (SG2)
C32S200ø8	W600S1L3	3	0.68	71.37	0.0181	2.17	6.03	0.0131 (SG1)	0.85 (SG1)
C32S300ø8*			1.06	71.56* 93.59**	0.0168	2.18* 2.86**	5.60	0.00718 (SG1)	0.46 (SG1)
C32S200ø8*	W600S1L5	5	1.13	71.51* 98.36**	0.014*	2.18* 2.99**	4.67	0.00735 (SG1)	0.47 (SG1)
C32S300ø8*			1.76	71.88* 111.1**	0.0121	2.19* 3.27**	4.03	0.00188 (SG1)	0.12 (SG1)

Table 3. Main indicators of the efficacy of the confinement systems in the C32S200\u00f68 and C32S300\u00f68 test series.

\* Values recorded when the load carrying capacity of the equipment was attained, without the occurrence of the failure of the specimens \*\* Values at the failure of the specimen

#### 4 THE MODEL

Although several confinement models have been proposed to simulate the stress-strain compression response of full FRP-wrapped concrete elements [1-5], there is a dearth of models able to accurately predict the behaviour of concrete columns confined by discrete CFRP arrangements. In the present work, the principles proposed by Harajli *et al.* (2006) were used to develop a confinement model to simulate, not only full wrapped specimens but also those confined with discrete arrangements.

The model, herein proposed, is based on the two stress-strain branches schematically represented in Figure 2. Point A, characterized by an  $\varepsilon_{cA}$  strain and an  $f_{cA}$  stress, separates the domain between a marginal and a significant influence of the effective lateral confining pressure, provided by the CFRP confinement arrangements,  $f_{fI}$ . Since the concrete volumetric expansion starts to occur before the compressive strength of unconfined concrete specimens, point A is evaluated upon a certain minimum value of the CFRP strain,  $\varepsilon_{f}$ .



Figure 2: Schematic representation of the stress-strain model for CFRP confined concrete

Based on the strains measured in the CFRP at the specimen axial level corresponding to  $\varepsilon_{co,URC}$  (strain at the compressive strength of unconfined reinforced concrete column, URC) a value of about  $3.0 \times 10^{-5}$  was assumed for  $\varepsilon_{f}$  to define  $\varepsilon_{cA}$  and  $f_{cA}$ . To obtain  $\varepsilon_{cA}$  and  $f_{cA}$ , as well as the  $\sigma_{c}$ - $\varepsilon_{c}$  points that define the second branch, the following equations are used [5]:

$$\sigma_{c} = f_{co,URC} + k_{1} f_{l} \text{ for } \varepsilon_{c} \ge \varepsilon_{CA}$$
<sup>(1)</sup>

$$\boldsymbol{\varepsilon}_{c} = \boldsymbol{\varepsilon}_{co,URC} \left[ 1 + k_{2} \left( \frac{\boldsymbol{\sigma}_{c}}{f_{co,URC}} - 1 \right) \right] \text{ for } \boldsymbol{\varepsilon}_{c} \ge \boldsymbol{\varepsilon}_{cA}$$
(2)

where

$$f_l = f_{fl} + f_{sl} \frac{A_{cc}}{A_g} \tag{3}$$

is the effective lateral confinement pressure, and  $k_1$  and  $k_2$  are two parameters that are obtained from the experimental results, [6]. In Eq. (4) and (5)  $f_{fl}$  and  $f_{sl}$  represent the effective lateral confining

pressure exerted by CFRP and ordinary steel hoops, respectively, and can be determined from the following equations:

$$f_{ff} = \frac{\alpha_{fe} \, \alpha_{fv} \, \rho_f \, E_f}{2} \, \varepsilon_f \tag{4}$$

$$f_{sl} = \frac{\alpha_{se} \,\alpha_{sv} \,\rho_{st}}{2} \,f_{syt} \tag{5}$$

where  $\rho_f$  is the CFRP volumetric ratio,  $E_f$  is the CFRP elasticity modulus,  $\rho_{st}$  is the volumetric ratio of steel hoops (Mander *et al.* 1988),  $\alpha_{fe}$  and  $\alpha_{fv}$  are the coefficients that account for the effectiveness of the FRP systems in the confinement of the concrete along the specimen cross section's plane, and the concrete between steel hoops, respectively [7]:

$$\alpha_{fv} = \frac{\left(1 - \frac{s_f}{2D}\right)^2}{1 - \frac{A_{sl}}{A_g}} \tag{6}$$

and  $\alpha_{se}$  and  $\alpha_{sv}$  are the coefficients that account for the effectiveness of the steel hoops in the confinement of the concrete along the specimen cross section's plane, and the concrete between steel hoops, respectively [7]:

$$\alpha_{sv} = \frac{\left(1 - \frac{S_s}{2 d_{st}}\right)^2}{1 - \frac{A_{sl}}{A_v}}$$
(7)

For circular columns  $\alpha_{te}=\alpha_{ve}=1.0$ , and for full wrapping configuration  $\alpha_{tv}=1.0$ . In Eqs. (6)  $s_t$  and D are, respectively, the clear spacing between consecutive FRP strips (for full wrapping  $s_{t=0}$ ) and the diameter of the specimen cross section, while  $s_s$  and  $d_{st}$  of Eq. (7) are, respectively, the steel hoop spacing and the diameter of the steel hoop. In these two equations,  $A_{st}$  is the cross section area of the longitudinal reinforcement and  $A_q$  is the area of the specimen cross section.

To obtain values for  $k_1$  of Eq. (2), the results obtained experimentally between  $k_1 = (\sigma_c - f_{co,URC})/f_1$  and  $f/f_{co,URC}$  are plotted in Figure 3. The size of the markers, which was used to distinguish values between the four series of the group of tests, is proportional to  $\rho_f$  (see tables 2 and 3).



Figure 3 – Variation of the confinement parameter  $k_1$  with the lateral confining pressure for: (a) C16 and (b) C32 series of tests.

For the C16 and C32 concrete strength levels adopted in the present work (this range is representative of the concrete of structures requiring strengthening intervention) the following equations for  $k_1$  were obtained:

 $k_1$ 

$$= a \left( \frac{f_l}{f_{co,URC}} \right)^{-b}$$

(8)

$$a = 2.9 + 72.848 \left( \rho_f - 0.0025 \right); b = 0.2177 \text{ for C16 and } \rho_f \in [0.0025; 0.0176]$$
  
$$a = 2.0 + 125.828 \left( \rho_f - 0.0025 \right); b = 0.42 - 7.947 \left( \rho_f - 0.0025 \right) \text{ for C32 and } \rho_f \in [0.0025; 0.0176]$$

For concrete specimens of  $f_{co,URC}$  inside of the strength range of C16 and C32 the  $k_1$  value can be obtained from linear interpolation using the  $k_1$  values determined from (8).  $k_{1-sup}$  and  $k_{1-inf}$  of C16 and C32 concrete strength classes were obtained from Eq. (8) attributing to  $\rho_f$  the values 0.0176 and 0.0025, respectively.

To obtain  $k_2$  of Eq. (2), the results registered experimentally between  $k_2 = (\varepsilon_0/\varepsilon_{co,URC} - 1)/(\sigma_0/f_{co,URC} - 1)$  and  $\varepsilon_f$  are plotted in Figure 4.



Figure 4 : Variation of the confinement parameter  $k_2$  with the lateral strain.

Based on the obtained results, the following equations were obtained for C16 and C32 concrete strength classes, respectively:

$$k_2 = \left[555 - 29006 \left(\rho_f - 0.0025\right)\right] \varepsilon_f + 2.0 \text{ for C16 and } \rho_f \in \left[0.0025; 0.0176\right]$$
(10)

$$k_2 = \left[ 600 - 28695 \left( \rho_f - 0.0025 \right) \right] \varepsilon_f + 1.0 \text{ for C32 and } \rho_f \in \left[ 0.0025; 0.0176 \right]$$
(11)

For concrete specimens of  $f_{co,URC}$  within the strength range of C16 and C32 the value of  $k_2$  can be obtained from linear interpolation using the  $k_2$  values determined from (10) and (11). ). K<sub>2-sup</sub> and k<sub>2-inf</sub> of C16 and C32 concrete strength classes were obtained from Eqs. (10) and (11) attributing to  $\rho_f$  take the values 0.0176 and 0.0025, respectively.

The model and the experimental stress-strain axial relationships ( $\sigma_c \cdot \varepsilon_c$ ) are compared in Figure 5. In this figure, compressive strains and stresses are considered as positive values. From the analysis of the represented curves it can be concluded that the developed model is able of predicting, with high accuracy, the axial compression behaviour of CFRP-based confined columns.

The performance of the proposed model was also appraised by simulating the tests carried out by other researchers ([4], [8]). A remarkable agreement between the model and the experimental stress-strain curves is apparent in figure 6. The results predicted by the models proposed by other researcher are also represented in this figure. It can be concluded that the developed model predicted with higher accuracy the experimental results than the predictions of previous models.

## **5 CONCLUSIONS**

The model developed by Harajli et al. to simulate the stress-strain relationship of concrete specimens confined with CFRP was modified in order to be capable of simulating the confinement provided by discrete CFRP-based arrangements. The developed model simulated accurately the stress-strain responses recorded in the experimental program carried out in the ambit of the present work, as well as the tests executed by other researchers.

In comparison to the prediction performance of other available models, the model developed in this study showed higher accuracy on the simulation of CFRP-based confined RC columns of circular cross section.

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Figure 5: Comparison between the model predictions and the experimental results for the: (a) C16S200\u00f68; (b) C16S300\u00f68; (c) C32S200\u00f68; (d) C32S300\u00f68.



Figure 6: Comparison between the model predictions and the experimental results of Triantafillou and Lam and Teng.