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# Influence of the incorporation of phase change materials on temperature development in mortar at early ages: Experiments and numerical simulation

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# HIGHLIGHTS

• New strategy for incorporating pristine PCM into the mortar.

• Strength of the PCM mortar is reduced but compatible with structural use.

• Quantitative experimental confirmation of PCM effectiveness in reducing the hydration induced temperature rise.

• Validation of numerical simulation capacity for early temperature development in mortar.

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# ABSTRACT

The present work is focused on a thorough experimental campaign to assess the thermo-physical properties and performance of mortar containing phase change materials (PCMs) with peak melting temperature of 34 °C. This selected melting temperature was targeted to reduce the peak temperature developed in mortar at early ages, induced by heat of hydration of cement. Indeed, 34 °C is well above normal casting temperatures, yet well below peak temperatures normally attained in massive concrete structures: therefore, this choice would represent a somewhat generalizable choice for attenuating peak temperatures. Due to experimental constraints, the tests conducted herein were performed on mortar (smaller size specimens are possible). However, the methods and findings may easily be extrapolated to concrete.

New preparation and incorporation protocols have been considered for using PCMs into mortar: (i) grated pristine PCM to be dispersed into mixtures; and (ii) macro capsule core of PCM. Three PCM volume fractions of 0, 10 and 20% using the two above mentioned different strategies of incorporation into the mortar were used to prepare a total of five mortar test prototypes. Furthermore, mechanical tests were then carried out on companion specimens to evaluate the effect of incorporating PCM on the compressive and flexural strengths.

The addition of grated PCM (i.e. shredded) in mortar led to enhancement of volumetric heat capacity while maintaining acceptable structural strength. The results revealed that the addition of PCM reduces density, thermal conductivity, and mechanical strength. In respect to the strength reduction, such percentages of incorporation were found to be small enough (<50%) as to not compromise the use of such mixtures for structural application.

As expected the tested PCM mortar specimens had a lower peak temperature, as compared to that of the reference specimens (mortar without PCM). Indeed, the 20% dispersed PCM mixture allowed peak temperature to decrease from  $\sim$ 52 °C to  $\sim$ 44.8 °C.

Complementarily, numerical models were developed and calibrated using the experimental data. The comparison between numerical simulation (using DIANA software) and experimental results revealed a very good agreement of the temperature profiles in the early ages. This allows to validate the capacity of simulating temperature evolution within mortar containing PCM, as well as, to understand the contribution of PCM to reduce the temperature rise coupled with the cement hydration phenomenon. It also represents a baseline methodology for scientists and practitioners to perform parametric analyses for other situations.

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# 1. Introduction

In concrete, the stress developed at early ages, which can lead to cracking (normally up to 7–14 days after mortar placement), is due to the restrained volume changes, originally associated with different factors [1]: (i) autogenous shrinkage which is induced by water consumption by the hydration process; (ii) drying shrinkage which is induced by evaporation of water during curing period; (iii) thermal expansion/contraction that is due to poor heat dissipation produced by the cement hydration and processes of temperature rise and cooling down of mortar. Early age cracking of mortar [2] may reduce the serviceability and durability [3].

Some strategies such as internal curing, use of specific cements and shrinkage admixtures have been developed to mitigate early age cracking [4]. Most recently, and specifically focusing on thermal cracking, a growing number of research studies have proposed the use of phase change materials (PCMs) as additives [5–9].

The principle of operation of PCMs [10] through heat storage in the scope of mortar applications can be explained with an example: in a concrete mixture containing PCM, when increasing core temperature of concrete (induced by cement hydration heat), temperature reaches the melting point of the PCM, it endures the corresponding phase change and absorbs heat (endothermic process), thus limiting the increase of temperature caused by cement hydration. Therefore, while the heat storage capacity of PCM still exists, concrete temperature tends to remain in the vicinity of the PCM's melting point [5], therefore limiting the temperature rise, and having smaller thermal cracking risk.

Some researchers have investigated methods of incorporation of PCM into cement based materials at laboratory and real scale levels: suspension of phase change material (SPCM) in combination with water [6], self-compacting concrete cubes containing PCMs (dispersed form of incorporation) [11], concrete containing porous aggregates incorporated with PCMs (in the form of vacuum impregnation) [12], mortar and concrete mixes blended with microencapsulated PCM (by direct incorporation) [13], footing member and bridge pier containing PCM (added into the mixture) [14], and cement based materials incorporating microencapsulated PCM [15].

A suitable phase change temperature and a large melting specific enthalpy are two of the main desirable requirements for PCM selection, among other properties. In order to design and optimize the thermal behaviour of a system based on latent heat storage through incorporation of PCM, an adequate knowledge of thermo-physical properties of commercially available or customized PCMs is necessary [16].

Based on the literature review in the scope of the present research, no previous works were found to have focused on the use and comparison of grated PCM and macro capsule core PCM for temperature control in structural concrete. Therefore, in the present research, these two methods of PCM incorporation were compared with a reference case (mortar without PCM) targeting the reduction of hydration-induced temperature swings in concrete at early ages.

For thermal performance testing, five cube prototype mortar specimens were prepared (edge of specimen with 20 cm length). Two specimens incorporated grated PCM (partial replacement of aggregates by PCM at 10% and 20% volumetric percentage), which was directly added into the mixture and casted into a cube proto-type. Two other specimens incorporating PCM as an inner macro capsule core (with 10% and 20% in volume measured in the same manner as the grated PCM) were studied. A reference mix (without PCM) was also cast into a cube prototype under the same conditions to establish a base for comparison. All specimens were placed under controlled climatic conditions and thermally insulated, as to

ensure that the inner temperature development resembled a realistic inner temperature development, similar to the one expected in a real-scale concrete structure.

The development of reliable numerical models and simulations of the transient thermal behaviour of mortar/concrete incorporating PCM is a relevant matter, mostly due to the need to be able to predict performance in scenarios that differ from the limited number of situations analysed through experiments [17].

In the scope of the present study a numerical model was developed using DIANA software [18]. This allows comparison of transient thermal simulation results with the experimental data results of the laboratory specimens for validation purposes. The numerical results of PCM mortar specimens were compared with the reference case (without PCM) to assess their effectiveness over the temperature profiles during the early ages, where generated heat due to the hydration of cement in the mixture occurs at different interfaces and for the whole cross-section of the cubes.

# 2. Experimental work

# 2.1. Materials and formulations

#### 2.1.1. Choice of phase change material

The selection of the melting temperature for the PCM for incorporation into the mortar was chosen based on existing knowledge of typical temperature development observed in practice for concrete structures (particularly massive ones). Therefore, the initial selection of PCM material was limited to those exhibiting phase change between 30 °C and 40 °C, which is a range that is likely to be attained in most concrete massive structures [16], when a casting temperature surrounding 20 °C is presumed.

Following the five cement classes defined by ASTM C 150 [19], the typical heat of hydration of Portland cement types I, II, III, IV and V are 350 kJ/kg, 265 kJ/kg, 370 kJ/kg, 235 kJ/kg and 310 kJ/kg, respectively. For discussion purposes, it can be stated that, the average hydration heat of cement is about 300 kJ/kg. Therefore, the selected PCM needs to have a high latent heat capacity and adequate dosage, when compared to 300 kI/kg brought by cement in the actual mixture, to provide a relevant enough heat absorption effect [3]. Based on the reasoning made so far, pristine PCM named "RT35HC" (from RUBITHERM paraffin RT series) [20] was selected as it is readily available in the market, it does not interact with other concrete/mortar mixture constituents, and also because it can absorb large amount of heat during phase change process [21]. RT35HC has melting temperature ranges between 34 °C and 36 °C with heat storage capacity of 240 kJ/kg, specific heat capacity of 2 kJ/kg K, density in solid state of 880 kg/m<sup>3</sup> and density in liquid stage of 770 kg/m<sup>3</sup>, according to the information provided by supplier [20].

#### 2.1.2. Mix design of the mortars

Portland cement type I class 42.5R is adopted as the binder from the SECIL company, in Outão, Portugal. River sand was used as inert filler. The grain size distribution of the sand is presented in Fig. 1. The fineness modulus of the sand was 3.2 mm. The preconditioning of all the materials was done according to the recommendations of the RRT<sup>+</sup> program of COST Action TU1404 [22].

The selected PCM (RT35HC) for this research was subjected to DSC experiment in order to provide information on the specific heat capacity of the PCM. A sample with weight of 7.564 mg of PCM (RT35HC) was used. The used DSC equipment (apparatus model Perkin Elmer) has an accuracy of  $\pm 0.3$  °C. The specific heat capacity was determined following the methodology detailed in Ref. [23]. A heating rate of 2 °C min<sup>-1</sup> was considered. The applied program steps for the test procedure of the sample was the

following: (i) initial isothermal period at 5 °C for 5 min; (ii) dynamic heating up to 50 °C according to the proposed rate (2 °C min<sup>-1</sup>). The sample was tested within aluminium crucibles with volume of 40  $\mu$ L under nitrogen (N<sub>2</sub>) atmosphere with a flow of 40 mL/min. The sample was weighed by an analytical balance with accuracy of ±0.01 mg. Sample was sealed in the pan by using an encapsulating press. An empty aluminium crucible was used as a reference.

The specific heat capacity of the PCM was obtained from the DSC. The volumetric heat capacity of the material is calculated by multiplying the real density  $(880 \text{ kg/m}^3)$  and specific heat capacity according to Eq. (1):

$$Cp v = Cp \times \rho \tag{1}$$

Such value ascribes the ability of the material in terms of energy storage in a certain volume while undergoing a gives temperature change. The result of volumetric specific heat capacity on sample taken from pristine PCM (RT35HC) is shown in Fig. 2. The melting peak temperature obtained of 36 °C. It is interesting to note that, the phase change melting temperature is in direct agreement with those specified by the material supplier [20].

Three different mixes have been prepared, without PCM and with different amount of grated PCM and macro capsule core PCM. The formulation of mortars with incorporation of grated pristine PCM allowed volume fraction substitution of 10 and 20% of the volume percentage of sand using replacement method.

Specific nomenclature has been given to each mortar mixture in order to facilitate identification. In this way, a designation type was created in which "REFM" stands for reference mortar (without PCM), "GPCMM10" stands for mortar incorporated with 10% Vol. grated PCM and "GPCMM20" stands for mortar incorporated with 20% Vol. grated PCM. The mix designs of the mortars studied herein, together with their adopted designations (REFM, GPCMM10 and GPCMM20) are presented in Table 1.

The flow table test was used to maintain the mixture workable according to the flow value based on dimeter of standard frustum. The workability tests were conducted through flow table test based on the European standard EN 1015-3 [24]. The mixture is considered workable only when the value of  $140 \pm 5$  mm was monitored/recorded for the proposed mixture. The workability tests showed that the incorporation of PCM leads to an increase in water content about 8% and 16% for the GPCMM10 and GPCMM20, respectively. This can be attributed to the reduced particle size of the used grated PCMs in the mixture compared to the sand



**Fig. 1.** Particle size characteristics of the sand: the distribution of particle size of the sand with the standard granulometry curve.



Fig. 2. Volumetric specific heat capacities calculated with the DSC outputs for the pristine PCM (RT35HC).

particles. Therefore, the performance of the mortars wease maintained at satisfactory level in the workability test.

In the scope of this work, a protocol was developed for embedding pristine PCM in the mixture for blends GPCMM10 and GPCMM20, as shown in Fig. 3. The pristine PCM was heated up to 40 °C to become liquid, see Fig. 3a, then steel containers were filled with liquid pristine PCM. They were then left to naturally cool down at room temperature (around 20 °C) for about 30 min (becoming solid, see Fig. 3b). Then, the PCM was demoulded from steel containers (Fig. 3c). Afterwards, the PCM blocks were grated (powder form, see Fig. 3d) and ready for use in to the mixtures. The granulometry curve for the PCM particles obtained through sieve analysis is shown in Fig. 3e. Fig. 3f, shows the detailed grain size distribution of the PCM. Materials including: Sand, cement, PCM and water were stored at a temperature of  $20 \pm 2$  °C prior to mixing. Tap water was used in the production of the mixtures. In order to check the temperature of materials, a laser thermometer (TESTO 875) was used to confirm the desired temperature range (20 ± 2 °C) for all materials before mixing.

# 2.1.3. Preparation procedures

The mixing procedure was based on the standard EN 480-1 [25]. Twelve prisms were made for each type of mortar (with 10% Vol. and 20%Vol. of grated PCM) including the reference mortar for comparison purposes. A total of thirty-six specimens were produced for the density measurement and mechanical tests (compressive and flexural strengths). Additionally, a total of five prototype cubes were produced for thermal tests: Reference mortar, PCM mortars with 10% Vol. and 20%Vol. of grated PCM dispersed in the mixture and PCM mortars with 10% Vol. and 20% Vol. of PCM in the form of a cubicle macro capsule core. It should be mentioned, that the thermal test for the reference mortar has been repeated in order to verify the repeatability of the result upon similar conditions.

The preparation of all mixtures was carried out according to the step-by-step procedure presented in Fig. 4. Firstly, the

Table 1Mix design of reference mortar and mortars with grated PCM.

Components (kg/m <sup>3</sup> )	Reference mortar	Grated PCM mortar	
	REFM	GPCMM10	GPCMM20
Cement Type I -42.5R (SECIL)	500	500	500
Water	245	265	285
Sand	1579	1435.5	1315.8
PCM	0	41.7	76.5



**Fig. 3.** Protocol for preparation of pristine PCM for incorporation into the mortar: (a) filling small containers from bulk PCM; (b) waiting about 30 min in the ambient temperature (20 °C); (c) PCMs in the form of solid; (d) grating pristine PCM; (e) sieving the PCM; and (f) distribution of particle size of ready to use PCMs with standard granulometry curve.

mixing of dry solid materials including sand, grated PCM and cement into a mixer for 30 s is carried out. Afterwards, adding water over the next 30 s, and continue the mixing process for an additional 150 s, stopping twice the mixing process to remove material from the mixer walls. Right after, the fresh mortar was cast into the moulds with respect to the type of the tests. The mortars were transferred to the steel moulds to produce specimens for future mechanical testing. Mortar casting for the thermal tests took place inside a climatic chamber with a constant temperature of 20 °C and relative humidity RH = 50%; data acquisition was started at the end of the casting operations. After 24 h, the specimens for the mechanical tests were demoulded. It should be mentioned that, for the production of the macro PCM capsule core, an aluminium foil (as a high conductive material) was used with a wall thicknesses about 1.6 mm in order to host the grated PCM in the shape of a macro capsule core PCM.

Specific nomenclature has also been given to the mixtures with macro capsule core of PCM in which "MPCMM10" stands for mortar with a cubicle macro capsule core filled with 10% Vol. of pristine PCM and "MPCMM20" stands for mortar with a cubicle macro capsule core filled with 20% Vol. of pristine PCM. It should be mentioned that, the volume size of the cubicle macro capsule cores for the formulations of MPCMM10 and MPCMM20 are the same ratios in terms of volume of grated PCM incorporation in the GPCMM10 and GPCMM20, respectively.

# 2.2. Characterization of mortars

Several experimental tests here was conducted to determine the thermo-physical properties of the studied mixture specimens in order to benchmark such properties related to the physical, mechanical and thermal properties of the mortars for use in the numerical simulations.



Fig. 4. Preparation procedures of specimens with grated PCM and macro capsule core PCM.

# 2.2.1. Density

For the density measurement, three specimens of each type were considered for each type of mixture. The test was following recommendations of EN1015:10 [26]. Firstly, the specimens were casted into prism moulds (with dimensions of  $160 \text{ mm} \times 40 \text{ mm} \times 40 \text{ mm}$ ). Then, the specimens were kept sealed with a plastic wrap at room temperature  $(20 \pm 1 \circ C)$  for 24 h. Then, the specimens were submerged at  $20 \pm 1$  °C for 7 days. Then, the specimens were dried at 70 °C until recording constant weight for each specimen. The dimensions of the specimens were measured using a digital calliper with a precision of 0.02 mm, and their weights were measured using an analytical balance with a precision of 0.001gr. Density values for REFM, GPCMM10 and GPCMM20 were 2188 kg/m<sup>3</sup>, 1904 kg/m<sup>3</sup> and 1870 kg/m<sup>3</sup>, respectively. Regarding the density difference between REFM, GPCMM10 and GPCMM20, it is interesting to note that the density of GPCMM10 and GPCMM20 are about 87% and 83% of that of REFM. In fact, the reduction of density for PCM mixtures were expected in view of the relevance of PCMs in the mixture which have lower densities than the sand particles.

#### 2.2.2. Thermal conductivity

The thermal conductivity of the specimens was determined in three representative specimens for each mixture formulation. The measurements were carried out through a steady state heat flow meter apparatus (Mathis, model TCi), according to ISO8301:1991 [27]. Mixtures were casted into prism moulds with dimensions of  $40 \times 40 \times 80 \text{ (mm}^3$ ), which were sealed and cured for 28 days at 20 °C. The apparatus is based on the modified transient plane source technique for measurement of thermal conduc-

tivity. It uses a one-sided, interfacial, heat reflectance sensor that applies a momentary, constant heat source to the specimen. The observed thermal conductivity of specimens GPCMM10 (0.4 W/m K) and GPCMM20 (0.3 W/m K), were significantly lower than that of REFM (0.5 W/m K). In fact, the PCM acts as insulating thermal material.

#### 2.2.3. Compressive strength

The compressive strength tests were performed to evaluate the effect of the PCM on the mechanical strength of the mortars. First, a series of the specimens were deployed for each mix in which three specimens were tested at the proposed ages of testing (7, 14 and 28 days) at room temperature (20 °C). The testing recommendations of EN1015-11 [28] were followed. All the specimens were kept sealed in a plastic wrap under at laboratory environment until testing date of 7, 14 and 28 days. Then, the compressive strength tests were carried out using apparatus model SHIMADZU-AG-IC with the capacity of 100 kN. For the compressive strength measurement, three specimens were considered for each type of the mortar and average values are reported.

Fig. 5 shows the compressive strength values in different specimens. The PCM incorporated in the mortar, as expected, reduces the compressive strength. The compressive strength of the GPCMM10 specimen in compare with REFM at 28 days is reduced by 18.6%. Such trend is in the line with the literature: [29–31]. For all specimens, the average 28 days are 21.2%, 24.3% and 26.5% higher than the average 7 days, for REFM, GPCMM10 and GPCMM20 specimens, respectively. The strength of the GPCMM20 was reduced about 50% in comparison with REFM specimen. The replacement of 20% of sand volume significantly reduces the strength of the mortar. The compressive strength of GPCMM10 at 28 days attained about 32 MPa that is still a reasonable value for the use in structural applications [32].

### 2.2.4. Flexural strength

Flexural strength testing was performed at ages of 7, 14 and 28 days following the standard EN1015-11 [28]. Three prism specimens with dimensions of  $40 \times 40 \times 160 \,(\text{mm}^3)$  were prepared and sealed by plastic wrap in room temperature (20 °C) until testing. A three-point loading method was deployed using apparatus model SHIMADZU-AG-IC with the capacity of 100kN. For the flexural strength measurements, three specimens were considered for each type of mixture and average values are reported. The trend of the flexural strength is similar to the observed for the compressive strength (see Fig. 6). The flexural strength of 6 MPa was measured for GPCMM10 and 4.5 MPa for GPCMM20 at 28 days. The addition of PCM also resulted in the reduction of the flexural strength. The flexural strength at 28 days for specimens GPCMM10 and GPCMM20 is significantly reduced in comparing with REFM by 23.8% and 42%, respectively. Similar behaviour was observed in previous studies by other authors: [11,33–35].

#### 2.3. Design and fabrication of the cube specimens

In order to assess the effect of different type of incorporating methods and quantities of PCM into mortar, for measuring early age temperature, five cube specimens were casted. The geometry of the cubes for the testing of REFM, GPCMM10 and GPCMM20 specimens, whose dimensions are  $200 \times 200 \times 200 \text{ mm}^3$ , is presented in Fig. 7. Lateral faces, base and top of the element were



**Fig. 5.** Compressive strength of mixture specimens for different curing time (for each mortar type, three specimens were tested and the average and standard deviation of the measured values are shown).



**Fig. 6.** Flexural strength of mixture specimens for different curing time (for each type of mortar, three specimens were tested and the average and standard deviation of the measured values are shown).

insulated with 40 mm thick extruded polystyrene (XPS) and 20 mm thick plywood formworks. For the PCM macro capsule core specimens, MPCMM10 and MPCMM20, an aluminium container (with high thermal conductivity) was used to host the pristine PCM with interior dimension of 75 mm<sup>3</sup> and 92 mm<sup>3</sup> for cases MPCMM10 and MPCMM20 specimens, respectively. For the sake of brevity, only schematic representation of the experimental set up for macro capsule core PCM mixture (MPCMM10) presented in Fig. 8. Mixture casting and the experimental procedures took place inside a controlled climatic chamber with a constant temperature of 20 °C and relative humidity of 50%. Data acquisition started at the end of the casting operations.

Regarding the experimental monitoring equipment, temperature sensors type K (thermocouple) very easy to use and economical, with precision of ±1.1 °C, were placed at different locations: geometrical centre of the mortar, exterior surface (level of mid height), and the edge at different height of the mortar: (i) on the top corner level; (ii) on the mid corner level; (iii) on the bottom corner level, between plywood formwork and XPS layer, and exterior surface of the plywood formwork. It should be mentioned that, in the cases of macro capsule core PCM mortars, one sensor was placed at the geometrical centre of the aluminium container, and one on the interior wall and another on the exterior wall. In fact, an identical temperature profile is expected in the symmetrical position for the purpose of comparison of measurements. Sensor locations are schematically presented in Figs. 7 and 8. These nomenclatures of top corner of the mortar cube (TC), mid corner of the mortar cube (MC), bottom corner of the mortar cube (BC), mid height of exterior boundary of plywood formwork (M1), mid height between plywood formwork and XPS (M2), mid height between XPS and mortar (M3), mid height centre of mortar cube (MM), mid height exterior boundary wall of aluminium container (M4), mid height interior boundary wall of aluminium container (M5), and mid height centre of pristine PCM inside aluminium container (MP), will also be adopted in this paper, for the discussion of results.

A total of five experiments were conducted by submitting the specimens to the controlled climatic chamber with experiment lasting 4 days. The temperature sensor reading in the different locations of the specimens were collected through a computer based data acquisition system (AGILENT 34970A) with a rate of one measurement per 15 min, during the whole 4 days period of testing. The physical arrangement of this setup can be observed in the pictures shown in Fig. 9. In this figure it is also visible, the use of a "supporting mesh" below the cube specimens in order to ensure that heat losses through the bottom surface would be similar to those of the other surfaces (hence guaranteeing symmetry).

#### 2.4. Thermal performance of cube specimens

Temperature measured in the position BC, MC, TC and M3 of the REFM, GPCMM10 and GPCMM20 specimens are presented in Fig. 10. It can also be noted that, the temperature rise period begins after mortar casting and lasts for about one day, then, followed by the cooling down period that goes on until the fourth day, reaching thermal equilibrium between the mortar specimen and the climatic chamber environment. It can be noticed that sensors located at points BC, MC, TC and M3 recorded the peak temperatures for different ages for the cases of GPCMM10 and GPCMM20 when compared with REFM. As expected, the sensors in the mortar specimens containing more PCM content, have recorded lower temperatures regardless of the sensor location and slightly shifted towards the left (i.e. delayed in time). Furthermore, it is worth noting that mixtures containing PCM reveal the charging and discharging effects in phase change within the temperature range



Fig. 7. Schematic representation of the experimental set up for reference mortar (REFM) and distributed form of grated pristine PCM mortars (GPCMM10 and GPCMM20): mixtures and sensor locations (labelled as "•"). Units [cm].

33–36 °C, both during ascending and descending branches of the temperature plots.

In the cases of GPCMM10 and GPCMM20 the maximum peak temperature reduction was recorded at point TC by  $\sim5$  °C and  $\sim9$  °C when compared with REFM, respectively (see Fig. 11).

Fig. 12 shows comparison of temperature profiles between cases of MPCMM10 and MPCMM20. The observations are quite similar to those already stated for GPCMM10 and GPCMM20 mortar specimens.

It can be noticed that sensors at points BC, MC, TC and M3 always measured peak temperature delay in the case of MPCMM20 in comparison with MPCMM10, opposed to those that were observed for the cases with PCM in the dispersed form (see Fig. 12). The maximum and minimum peak temperature differences between MPCMM10 and MPCMM20 were of 3.9 °C and 2.4 °C at BC and TC sensor points, respectively (see Fig. 13).

Generally, it can be observed that the PCM always leads to the temperature profile attenuation. The temperature profile at e.g. control point (M3) for the two methods of PCM incorporation that were assessed, have revealed to effectively reduce the peak temperature. However, the type of incorporation of PCM into the mixture is very effective in term of surface temperature profile evolution during early ages (in particular differences in rising temperature ramp of MPCMM20 and GPCMM20 is clearly noticeable). However, the temperature rise for all PCM cube specimens resemble the same attenuation and delay trend, as shown in Figs. 10 and 12.

Fig. 14 shows measurements from the thermocouples placed along different layers of the specimens in the middle height level. It can be observed that, the surface temperature of the specimen (M1) is almost constant for all cases due to the set point considered for climatic chamber as of 20 °C. Temperature monitoring between



**Fig. 8.** Schematic representation of the experimental set up for macro capsule core PCM mortar specimen (MPCMM10): mixture and sensor locations (labelled as "•"). Units [cm]. In the case of specimen MPCMM20, interior size of aluminium container was of 9.2 cm<sup>3</sup> with similar conditions as for specimen MPCMM10.

plywood formwork and XPS (M2) indicated the influences of the thermal insulation around cubic mortars experienced lower temperature (below 25 °C) for different studied cases. It is worth noting the strong coherence of temperatures measured by the thermocouples positioned at M3 and MM for the cases of GPCMM10, GPCMM20 and REFM. In fact, the placement of these thermocouples is along two symmetrical plans of the mixture element for REFM, GPCMM10 and GPCMM20. In the cases of MPCMM10 and MPCMM20, the monitored temperatures at intersection of the symmetrical plans (MP) shows the flatter effectiveness of the PCM due to it is specific heat capacity of the PCM. Measured temperatures at M4 and M5 in cases of MPCMM10 and PCMM20 are also coherence confirming the material used for

PCM container had no effect on the heat transfer between aluminium container and mixture. However, there is slight disturbance observed in the case of MPCMM20.

# 3. Numerical simulation

# 3.1. Governing equations

The general transient heat conduction equation [36] was applied for the numerical simulation of the heat transfer processes in the studied models:

$$k\nabla .(\nabla T) + Q = \rho C T \tag{2}$$



Fig. 9. (a) Photo of the prototype within climatic chamber before starting the test; (b) position of the temperature sensors for GPCMM10 and GPCMM20 cases; (c) position of the temperature sensors for MPCMM10 and MPCMM20 cases.



Fig. 10. Comparison between change of interior corner temperature and control point between REFM, GPCMM10 and GPCMM20: (a) point BC; (b) point MC; (c) point TC; and (d) M3 point.



Fig. 11. Peak temperature reduction between reference mortar (REFM) and PCM mortars (GPCMM10 and GPCMM20) at BC, MC, TC and M3 positions.

where Q is the rate of internal heat generation (W/m<sup>3</sup>) generated by cement hydration, k is the thermal conductivity and  $\rho C$  is the volumetric specific heat (J/m<sup>3</sup>K) of the mortar. Q plays a fundamental role on the thermal problem to be solved, and accordingly it should be determined on real characterization of the cement hydration heat production, considering activation energy phenomena (thermally-activated). As the same type of cement, from the same supplier had been tested and reported before [37] through isothermal calorimetry testing (including evaluation of activation energy), the corresponding results have been used as input for the models of simulation of this paper. The simulation of the heat generation was made with basis on an Arrhenius law of the type [16]:

$$\dot{O} = af(\alpha)e^{\frac{E_a}{RT}} \tag{3}$$

where  $E_a$  is the activation energy (J/mol), R in the universal gas constant (8.314 J/mol K), a is proportional to the maximum value of the heat production rate (W/m<sup>3</sup>) and  $f(\alpha)$  is the evolution of normalized heat production rate. It is worth to mentioned that, the degree of heat development  $\alpha$ , in the numerical simulation definition is the level of completion of the release of cement hydration heat which, in the case communicated herein, evolves from 0.1 (at initiation of simulation, considering release of heat before placement into mould) up to 1. The formulation of  $\hat{Q}$  assumes no chemical interac-

tion between cement and the PCM. This assumption is deemed feasible, as no opposing trend was found in the literature on this subject.

In regard to boundary conditions applied to the temperature field computation based on Eq. (2), the corresponding heat flows are taken into account through a convective/radiative boundary flux, as shown in Eq. (4), where *T* is the temperature (°C),  $T_s$  is the surface temperature (°C) and  $h_{cr}$  a convection/radiation coefficient that depends on air speed (W/m K) [16]:

$$q = h_{cr}(T - T_s) \tag{4}$$



Fig. 12. Comparison between change of interior corner temperature and control point between MPCMM10 and MPCMM20: (a) point BC; (b) point MC; (c) point TC; and (d) M3 point.



Fig. 13. Peak temperature differences between MPCMM10 and MPCMM20 at BC, MC, TC and M3 positions.

#### *3.2. Phase change modelling*

In the present work, and for the particular case in which PCM is distributed within the mortar mixture, the strategy for simulation of the enthalpy of phase change consists in increasing the heat capacity value of the mortar during the phase change process, which is normally termed as 'specific heat capacity method' [38,39]. In the experimental curve of specific heat capacity versus temperature (see Fig. 4), the sensible heat and latent heat temperature ranges are not precisely distinguishable, thus, the specific heat capacity method could be beneficial as allows observing such curve/behaviour regardless state of the PCM. Hence, the effects of the phase change in this case (PCM distributed within the mortar mixture - GPCMM10 and GPCMM20) were modelled through a simplified approach by which the energy release/absorption associated to the phase change process is considered through artifacts



Fig. 14. Temperature measured by thermocouples on different positions of tested specimens: (a) GPCMM10, (b) GPCMM20, (c) MPCMM10, (d) MPCMM20, and (e) REFM.



**Fig. 15.** Estimated specific heat capacity curves of the PCM mortars based on the experimental results obtained for pristine PCM (RT35HC): (a) for GPCMM10; and (b) for GPCMM20.

applied to the specific heat capacity term shown in Eq. (2). This approach consisted in making a proportionality estimation, based on a simple mixing law, in order to extrapolate the expectable specific heat of mortar, following equation Eq. (5) [17]:

$$C_{specimen}(T) = (X_{mixture} \times C_{mixture}) + (X_{PCM} \times C_{PCM})$$
(5)

where  $C_{specimen}$  is the specific heat capacity of the mortar mixture containing PCM (kJ/kg K) as a function of temperature (T),  $X_{mixture}$ stands for mass fraction of the mortar mixture,  $C_{mixture}$  is the specific heat capacity of the mortar mixture (kJ/kg K),  $X_{PCM}$  is mass fraction of the PCM within matrix, and  $C_{PCM}$  is specific heat capacity of the PCM (as extracted directly from Fig. 4). The volumetric specific heat capacity for GPCMM10 and GPCMM20 was obtained by multiplying the previous result by the volumetric density of specimens are illustrated in Fig. 15 and ready for implementation in numerical simulation.

For the computation of the volumetric specific heat capacity of the macro capsule core PCM for the cases of MPCMM10 and



Fig. 17. Arrhenius law for the studied mixture.



Fig. 16. The 3D model mesh for: (a) REFM, GPCMM10 or GPCMM20; (b) MPCMM10; (c) MPCMM20.

 Table 2

 Thermo-physical properties of the materials used in the numerical simulations.

Thermo-physical properties	Units	REFM	GPCMM10	GPCMM20	XPS	Plywood	Pristine PCM
Density	(kg/m <sup>3</sup> )	2188	1904	1877	32	650	880
Thermal conductivity	(W/m K)	0.5	0.4	0.3	0.035	0.15	0.2
Volumetric Specific heat capacity	(kJ/m <sup>3</sup> C)	2189	Fig. 15a	Fig. 15b	44.8	854.4	Fig. 2



Fig. 18. Experimental versus numerical values for different models at control point (M3): (a) REFM; (b) MPCMM10; (c) MPCMM20; (d) GPCMM10; and (e) GPCMM20.

MPCMM20, the information of Fig. 4 was used directly for model input of the specific heat of the material, for application in Eq. (2).

# 3.3. Modelling geometry and parameters

The five cases presented in Section 2 were simulated: (i) REFM; (ii) GPCMM10; (iii) GPCMM20; (iv) MPCMM10; and (v) MPCMM20. The specimen with exterior dimensions of  $32 \times 32 \times 32$  cm<sup>3</sup> has been considered. Since there are three vertical symmetry plans, only one-eighth of the prototype with dimensions of  $16 \times 16 \times 16$  cm<sup>3</sup> was modelled. It is noted that

it was decided to explicitly model the XPS and formwork linings around the specimen due to the fact that they ended up storing some heat in the experiment (due to their relatively significant thickness in regard to the mortar specimen inside). The generated finite element mesh (eight noted isoperimetric finite element), is depicted in Fig. 16a–c. In the adopted 3D discretization finite elements renders element size of 0.05 cm for the cases of REFM, GPCMM10, GPCMM20 and MPCMM20, while, a quite refined mesh in the MPCMM10 with element size of 0.04 cm used. In the symmetry plans, adiabatic boundaries were considered.



Fig. 19. Temperature contours at instant when maximum temperature reached: (a) t = 0.65 day for REFM; (b) t = 0.67 day for MPCMM10; (c) t = 0.67 day for MPCMM20; (d) t = 0.8 day for GPCMM10; and (e) t = 0.8 day for GPCMM20, under proposed environmental condition.



Fig. 20. Temperature variations along the thickness of the wall of cube specimens at different hours: (a) GPCMM20; and (b) MPCMM20.

The main thermo-physical properties of all materials used in the simulations of REFM, GPCMM10, GPCMM20, MPCMM10 and MPCMM20 are synthetized on Table 2 and detailed next. This table also contains information about the materials that were used in the construction of the mould walls. It is noted that the specific heat capacity of mixture containing distributed PCM was estimated based on Eq. (6). It should be mentioned that, the characteristics of the MPCMM10 and MCPMM20 for simulation inputs are composed of the REFM and pristine PCM.

In regard to the boundary conditions applied to the temperature field computation, for the surfaces in contact with wooden framework panels,  $h_{cr}$  was of 5 Wm<sup>-1</sup> K<sup>-1</sup>. In the symmetry plans adiabatic condition were applied. A constant time step size of 300 s and number of time steps of 1152 were considered (4 days). The convergence criteria at each time step was checked under 10<sup>-5</sup> for energy equation.

The initial temperature for the cases of REFM, GPCMM10, GPCMM20, MCPMM10 and MPCMM20 were 19 °C, 18.5 °C, 18.5 °C, 18.5 °C, 17.5 °C, 16 °C, respectively, as recorded experimentally. Data for simulation of heat of hydration generation according to Eq. (4) is shown in Fig. 17. This information was taken from for CEM I 42.5R (CB), and a volumetric content of 500 kg/m<sup>3</sup> of cement was considered for volumetric expression of *a*. All calculations were performed using the DIANA software [40].

# 3.4. Results of the numerical simulations

The numerical approach towards simulation of PCM behaviour in both embedded and discrete conditions will be validated by comparing its predictions with experimental results, presented next. The comparison of experimental and simulation results at control node for different cases are shown in Fig. 18a-e. From the observation of Fig. 18a-e, it can be confirmed that the numerical predictions for the T-t evolution match quite closely the ones measured by the thermocouples in the cases of REFM, MPCMM10 and GPCMM20, thus, very good agreement between numerical and experimental results can be observed, which validates the assumed simulation strategy. However, there is slightly shifting to the right side can be noticed in the case of MPCMM10. However, in the cases of GPCMM10 and MCPMM20 the maximum differences in the peak temperature reaches to 1.4 °C and 0.7 °C, respectively. For every case, the temperature at the control point (M3) undergoes a rise to a peak due to cement hydration heat release and then a gradual decreasing trend up to the end.

Fig. 19 presents the temperature contours inside the models for the time frames when reached to their maximum temperatures. However, the temperature at the mortar layer is higher than centre of the model where the PCM located. Macro capsule core PCM causes change in the fashion trend for the counters, thus, allowing to lower temperature experiences by mortar part when compared with distributed form of the PCM into the mortar.

Typical specification for concrete includes a maximum temperature and a minimum temperature differential [41]. According to the temperature contours in the mixture parts at time steps of 0.65 day, 0.67 day, 0.67 day, 0.8 day and 0.8 day, temperature differences from the centre to the surfaces of the mortars are 7.3 °C, 1 °C, 2.8 °C, 6.1 °C and 6.2 °C for REFM, MPCMM10, MPCMM20, GPCMM10 and GPCMM20, respectively, and such a temperature difference in the simulated cases with PCM incorporation may not lead to cracking, as temperature differential is reduced.

In order to further illustrate the effect of PCM in the mortar, Fig. 20 shows the calculated temperature profiles in the wall layer of the GPCMM20 and MPCMM20 at several instants within given environmental conditions. The selected instants that range 0.4 day–2.6 day (involves a heating/cooling ramp) for the case of GPCMM20 show that the mortar layer is enduring a quasiisothermal state at such stage (absorbed by latent heat storage/ release), while the temperatures in the outer layers (insulating materials) has significant gradients. This is due to the melting / solidification temperature ranges of used PCM in mortar which has onset temperature around 30 °C and end temperature around 40 °C, as identified by horizontal dashed lines in Fig. 20a. Macro capsule core of PCM caused more uniform mortar's temperature profile within melting/solidification temperature range, along the mortar layer (see Fig. 20b). Similar findings and conclusions can be observed by analysis of the GPCMM10 and MPCMM10 specimens.

The fact that the temperature simulations in all cases match well, the measured values seems to further confirm the assumption that the heat generation function is not affected by the presence of PCM, as mentioned in Section 3.1 (even in the case of non-encapsulated PCM where direct contact with cement was possible).

# 4. Conclusions

In this research, mortars incorporating grated PCM and macro capsule core of PCM have been developed and experimentally characterized. Based on the test results, the following main conclusions can be drawn:

- The addition of grated pristine PCM into the mortar has led to 13% and 17% reduction of the density when compared with the reference mortar (without PCM). These mortars incorporating PCM comply with the light weight mortar values for construction applications, where for example, a lower dead load value of the structure is desirable.
- The thermal conductivity values for the PCM mortars was reduced by 20% and 40% for GPCMM10 and GPCMM20, respectively, when compared with the reference mortar due to the lower conductivity of PCMs.
- Adding PCM leads to the reduction of the average compressive and flexural strength, however it still presents values compatible with possible structural use. In fact, the addition of 10% and 20% grated PCM revealed a compressive strength of 32 MPa and 20 MPa, respectively, which is compatible with some structural applications.
- Overall thermal characterization tests have demonstrated the reduction of temperature rise, enhancement of thermal capacity of the mortar incorporating PCM.
- The heat transfer performance tests revealed that the dispersed form of PCM or macrocapsule cores of PCM has a beneficial effect over the heat gain energy.
- The heat release rate of cement hydration of mixtures with PCM were effectively changed by the two strategies of PCM incorporation into the mortars.
- Successful experimental validation was achieved, providing a transient thermal base model to predict temperature profile evolution within mortar containing PCMs in the both forms herein used.

From the calibrated numerical simulations using DIANA software it was also demonstrated that PCMs can reduce high temperature fluctuations in the early ages and flatten temperature swings in their melting temperature range. As a final note, this paper clearly proves that, through simulation tools, properly designed mortar/concrete mixes with plausible percentage of PCM incorporation in the mix have a significant potential to reduce temperature peaks/gradients induced by heat of hydration and have a positive contribution towards the reduction of thermal cracking risk in early ages. However, it is noted that further research is needed to assess the kind of trade-off brought about by the alterations in mechanical properties that is caused by the introduction of PCM in the mix: indeed, a reduction of tensile strength (and alteration of other properties) could potentially bring negative effects on the risk of cracking that diminish or even surpass the benefits attained by the temperature peak/gradient reduction achieved through PCM incorporation. These are however effects whose study will demand a dedicated research on several relevant properties of cement-based materials (mortar/concrete) containing incorporated PCM through the techniques mentioned in this paper (or others), namely E-modulus, creep behaviour, tensile strength, shrinkage, thermal expansion coefficient. Their intricate interplay in the thermo-mechanical behaviour of concrete at early ages would then require a combination of experimental validation (e.g. through use of a TSTM – Temperature Stress Testing Machine) and numerical simulation (thermo-mechanical analyses).

# **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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