Hybrid dynamic modeling of *Escherichia coli* central metabolic network combining Michaelis–Menten and approximate kinetic equations

Rafael S. Costa, Daniel Machado, Isabel Rocha, Eugénio C. Ferreira *

IBB-Institute for Biotechnology and Bioengineering, Centre of Biological Engineering, Universidade do Minho, Campus de Gualtar, 4710-057 Braga, Portugal

**Abstract**

The construction of dynamic metabolic models at reaction network level requires the use of mechanistic enzymatic rate equations that comprise a large number of parameters. The lack of knowledge on these equations and the difficulty in the experimental identification of their associated parameters, represent nowadays the limiting factor in the construction of such models. In this study, we compare four alternative modeling approaches based on Michaelis–Menten kinetics for the bi-molecular reactions and different types of simplified rate equations for the remaining reactions (generalized mass action, convenience kinetics, lin-log and power-law). Using the mechanistic model for *Escherichia coli* central carbon metabolism as a benchmark, we investigate the alternative modeling approaches through comparative simulations analyses. The good dynamic behavior and the powerful predictive capabilities obtained using the hybrid model composed of Michaelis–Menten and the approximate lin-log kinetics indicate that this is a possible suitable approach to model complex large-scale networks where the exact rate laws are unknown.

© 2010 Elsevier Ireland Ltd. All rights reserved.

1. Introduction

One of the great challenges in the post-genomic era is to understand the dynamic behavior of a living cell. For that purpose, quantitative models describing metabolic network dynamics are a powerful tool to explain properties of complex biological systems and to guide experimentation (Kitano, 2002). In this context, dynamic changes in metabolite concentration over time are predominantly simulated using non-linear ordinary differential equations (Bakker et al., 1999; Klipp et al., 2007) that require a previous knowledge on the network structure and a large amount of experimental information, such as initial concentrations of metabolites, kinetic parameters and detailed kinetic rate laws. Mechanistic kinetic rate expressions have been the usual approach in metabolic networks modeling. In the last years, several dynamic models have been developed and examples include the tricarboxylic acid cycle in *Dictyostelium discoideum* (Wright et al., 1992), the threonine synthesis pathway in *Escherichia coli* (Chassagnole et al., 2001), and the glycolysis in *Trypanosoma brucei* (Bakker et al., 1997). A major challenge with such models, however, is that they often possess many kinetic parameters. While information on network structure can be compiled from public databases (for example Karp et al., 2000; Ren and Paulsen, 2007), there are currently few methods for estimating kinetic parameters. In addition, kinetic parameter values measured in vitro may originate significant differences between simulated and experimental data because the conditions at which in vitro assays are performed are often different from those inside the cell (such as buffering conditions, temperature, intracellular pH, etc.) (Richey et al., 1987; Teusink et al., 2000). A common approach to address this issue has been the use of time course *in vivo* data in response to a stimulus (Theobald et al., 1997; Vaseghi et al., 1999; Wahl et al., 2006) for kinetic parameter estimation by minimizing a cost function (Mendes and Kell, 1998; Moles et al., 2003). However, despite a number of successful applications, this approach has several limitations due to parameter identifiability problems on mechanistic models. On the other hand, the true mechanistic kinetic rate law for a specific reaction is frequently not known for most of the enzymes.

For these reasons, the application of these approaches to kinetic models requires a large amount of experimental data and has been limited to biochemical networks of limited size (Ishii et al., 2007), with the exception of the human red blood cell model (Jamshidi et al., 2001). Alternatively, large-scale metabolic models can be constructed based on stoichiometry without large fitted parameter sets. Although these models can be used to predict steady-state behavior using flux analysis, they fail to capture the transient behaviors of metabolism. Recently, a great effort has been car-
ried out by researchers to develop alternative approaches to build large-scale models with incorporation of some dynamic phenomena. Dynamic flux balance analysis (DFBA) has been proposed for situations where there is kinetic knowledge available for part of the model (Mahadevan et al., 2002). Another hybrid approach was developed by Yugi et al. (2005). The proposed method aims to reduce the number of enzyme kinetic assays necessary to build a dynamic model, by considering a dynamic and a static part. The static module is simulated by metabolic flux analysis (MFA) constrained by the information obtained from the dynamic module. There are some limitations to be considered for accurate simulations, such as the need to know the elasticity coefficients at boundary reactions between modules and inconsistencies in the static module caused by the inclusion of irreversible reactions.

Another approach to overcome some of the difficulties in large-scale dynamic modeling is to use different alternative rate equations like linear-logarithmic (lin-log), logarithmic-linear (log-lin), or power-law kinetics (Hatzimanikatis and Bailey, 1996; Savageau, 1970; Visser and Heijnen, 2002), where the kinetic parameter values can be estimated from time course and/or steady-state experimental data (Nikerel et al., 2006; Vilela et al., 2008). Parameters of such alternative kinetics expressions can be also inferred from the stoichiometry of the reactions (Smallbone et al., 2007). The most important advantage of approximate rate equations is the relative small number of parameters, which consequently reduces the number of experimental assays necessary for their identification, while still giving a reasonable description of the in vivo system. These approximated kinetic expressions also have a uniform format and therefore reduced mathematical complexity.

A number of dynamic simulation studies of biochemical systems with simplified enzyme kinetics equations have been reported in the literature. Spieth et al. (2006) applied linear weight matrices, S-systems and H-systems models, and also different optimization algorithms to model a non-linear dynamic system. Wang et al. (2007) compared S-systems and lin-log models to represent an aspartase-overproducing E. coli strain in batch fermentations. Furthermore, Voit et al. (2006) combined in vivo metabolite data obtained with NMR techniques and Biochemical Systems Theory as modeling framework to analyze the dynamic behavior in Lactococcus lactis. However, the applicability of multiple kinetic rate types for modeling large-scale biochemical networks has rarely been investigated.

In this work, we explore alternative approaches based on mechanistic (Michaelis–Menten) and simplified alternative kinetics to the large-scale E. coli network (Chassagnole et al., 2002). We constructed four hybrid models where the mechanisms for reactions with one substrate have been considered to follow the Michaelis–Menten kinetics, while approximated kinetics have been used for the other reactions, such as, generalized mass action, convenience kinetics, power-law, and lin-log. These models were then compared with the full mechanistic reference model (Chassagnole et al., 2002). Finally, analysis of stability and prediction power has been performed to evaluate the best alternative modeling approach.

2. Methods

Dynamic modeling of biochemical networks has evolved substantially in recent times, aided by the arrival of completely sequenced genomes (Blattner et al., 1997), the development of high-throughput technologies to rapidly obtain quantitative measurements for multiple metabolites (Theohal et al., 1993; Visser et al., 2002), and the completion of publicly-available metabolic databases (Je et al., 2003; Karp et al., 2000; Schomburg et al., 2002; Sundararaj et al., 2004; Rojas et al., 2007). Non-linear ordinary differential equations (ODES) systems are the most commonly applied technique to model quantitatively a biochemical network. If we consider $n$ species, the generic form will come (Conrad and Tyson, 2006):

$$\frac{dc_i}{dt} = \sum_{j=1}^{m} N_{ij} r_j - \mu C_i$$

(1)

where $C_i$ is the concentration of metabolite $i$, $N_{ij}$ is the stoichiometric coefficient of metabolite $i$ in reaction $j$. The reaction rate $r_j$ of the $j$th reaction is given by non-linear expressions, which depend on the metabolite concentrations and kinetic parameters, $\mu$ is the specific growth rate and $m$ is the number of reactions in the network.

2.1. Reference Model

In this contribution, the full mechanistic model representing the central carbon metabolism of E. coli formulated by Chassagnole et al. (2002), available in SBML curated format at BioModels online database (Le Novère et al., 2006), was selected as a benchmark. The model integrates the reactions of glycolysis, pentose phosphate pathway, the phosphotransferase system (PTS), and several compound synthesis systems connected with these pathways that lead for biomass formation. The details of the metabolic network, the mass balances, the initial concentrations of the metabolites, and the list of mathematical mechanistic rate equations of the model can be found in the original paper (Chassagnole et al., 2002). The model accounts for 10 reaction rates, outlined in Table 1, with a total of 116 kinetic parameters and 18 metabolites. The co-metabolites were represented by time-dependent non-linear functions (Chassagnole et al., 2002). The model simulations using the deterministic LSODA solver (Petzold, 1983) were conducted during 40 s after a glucose impulse of 1.67 mM.

2.2. Kinetic Rate Equations for Dynamic Analysis

2.2.1. Michaelis–Menten

The Michaelis–Menten kinetics assume that the rate at which an enzyme binds to its substrate is much faster than the rate of the product formation, and that the intermediate reaction is therefore at steady-state (see for example Lauffenburger and Linderman, 1993). The reaction rate is dependent on the rate constants – Michaelis constant, $K_M$, and forward rate constant, $r_{max}$. The Michaelis–Menten rate expression can be applied to reactions with one substrate and one product (bi-molecular reactions), and the more complex expression considering inhibition (Cornich-Bowden, 1985; Heinrich and Schuster, 1996) can be written as:

$$r = \frac{r_{max}(K_M/K_{p1}) S - (r_{max}/K_{p2}) P}{1 + (S/K_{p1}) + ((P/K_{p2}) + (P/K_{p3})) + 1 + (K_{p2} + (P/K_{p3})})$$

(2)

where $K_{p1}$ and $K_{p2}$ are the Michaelis–Menten constants for the substrate and product, respectively. $K_{p2}$ and $K_{p3}$ are the inhibition constants. $r_{max}$ is the maximal forward reaction rate, and $r_{max}$, the maximal reverse reaction rate. $S$ and $P$ denote the concentrations of the substrate, product, and inhibitor, respectively. To describe the three inhibition effects the following limits are often used (Heinrich and Schuster, 1996): for competitive inhibition ($K_I = \frac{K_{P1}}{K_{P2}}$, 0 and $K_{P1} < \frac{K_{P2}}{K_{P3}}$), competitive inhibition ($K_I = \frac{K_{P1}}{K_{P2}}$, 0 and $K_{P1} < \frac{K_{P2}}{K_{P3}}$), and non-competitive inhibition ($K_I = \frac{K_{P1}}{K_{P2}}$, $K_{P1} < \frac{K_{P2}}{K_{P3}}$). If the mechanism of the reaction is not affected by an inhibitor and the thermodynamic equilibrium constant ($K_{eq} = r_{max}(K_M/K_{p1})/(1 + (P/K_{p2})) + S$) is known, then the rate law can be reduced to the following equation:

$$r = \frac{r_{max}(S - (P/K_{eq}))}{K_{eq}(1 + (P/K_{eq})) + S}$$

(3)

2.2.2. Approximate Kinetics Representation

In general, the precise enzyme kinetics rate laws are not known for all the enzymes and membrane transporters. The approximated kinetic representations that we propose are the generalized mass action (Horn and Jackson, 1972; Schauer and Heinrich, 1979), lin-log kinetics (Hatzimanikatis and Bailey, 1997; Visser and Heijnen, 2003), power-law models (Savageau and Voit, 1982), and the more recently developed convenience rate law (Liebermeister and Klipp, 2006).

2.2.2.1. Generalized mass action. The generalized mass action (GMA) represents the simplest rate law, in which the enzymes effects are hidden. This rate law requires the specification of only two rate constants, the forward rate constant ($k$) and the thermodynamic equilibrium constant ($K_{eq}$). The value of the constant $k$ takes into account all unknown effects influencing the enzyme, like the allosteric effectors or molecular crowding. If inhibition and/or activation are involved, a positive pre-function has to be applied, as suggested by Schauer and Heinrich (1983) and Liebermeister and Klipp (2006). Therefore, the rate equation takes the following form:

$$r = k P \sum_{i=1}^{n} \left( A_i \sum_{i=1}^{n} \left( 1 + K_{a} \right) \right) \left( \prod_{i=1}^{n} \left( 1 + K_{b} \right) \right) \left( 1 \prod_{i=1}^{n} \sum_{i=1}^{n} P_{i} \right)$$

(4)
where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)

where the superscripts (0) denote the reference state (e.g. wild type at steady-state),  

$$ r_i = \frac{r_i}{r_i^0} \left( 1 + \sum_{i=1}^{nS} \alpha_i \ln \left( \frac{S_i}{S_i^0} \right) + \sum_{j=1}^{nP} \beta_j \ln \left( \frac{P_j}{P_j^0} \right) \right) $$(5)
2.2.2.4. Convenience kinetics. The most recently developed semi-mechanistic rate law was formulated from a simple random-order enzyme mechanism and can be applied to any reaction catalyzed by an enzyme. This rate law is a particular case of the generalized mass action kinetics (for details on the equation derivation see Liebermeister and Klipp, 2006). The general representation of this equation is described by:

\[
\frac{\partial \mathbf{c}}{\partial t} = \mathbf{Q} \mathbf{r} - \mathbf{S} \mathbf{c}
\]

where \( \mathbf{r} \) is the pseudo-experimental data of a given \( i \) metabolite concentration and \( y_i \) is the concentration given by the model at the \( j \)th sampling point and \( s \) is the number of metabolites. Each distance is normalized to overcome the different orders of magnitude of the metabolite concentrations.

2.4. Model Ranking and Selection

The mean relative error (MRE) was used to evaluate the performance of each alternative modeling approach, defined as (Kitayama et al., 2006):

\[
\text{MRE} (%) = \left( \frac{\sum_{i=1}^{s} \sum_{j=1}^{t} |x_{ij} - y_{ij}/x_{ij}|}{st} \right) \times 100
\]

where \( x_{ij} \) is the pseudo-experimental data of a given \( i \) metabolite concentration and \( y_{ij} \) is the concentration given by the model at the \( j \)th sampling point and \( s \) is the number of metabolites.

3. Results and Discussion

For large-scale kinetic models we need extensive knowledge on the stoichiometry of the metabolic network, the kinetic parameters and detailed rate laws. An integration of these three types of information will in principle allow to describe the rate of change for each metabolite. However, it is often very difficult to determine the functional form of the rate equations for the majority of the biochemical reactions and their associated kinetic parameters. A general principle when building kinetic models is to make the model as simple as possible, while capturing the realistic dynamic behavior (Dano et al., 2006). As such, some alternative strategies have been proposed (Famili et al., 2005; Yugi et al., 2005). The motivation for this work is to evaluate alternative kinetic modeling approaches containing fewer kinetic parameters in a large-scale network. For this purpose, we compare four hybrid models combining Michaelis–Menten for bi-molecular enzyme reactions rate laws and approximate rate equations with the full mechanistic reference model for the central carbon metabolism of E. coli proposed in Chassagnole et al. (2002). By developing these kinetic models it was possible to simulate the entire E. coli network.

3.1. Comparison of the Modeling Approaches

The reactions, number of parameters, and the type of kinetic mechanism for each biochemical reaction in the reference model are summarized in Table 1. Due to the approximation assumptions of the alternative rate equations we have applied Michaelis–Menten equations whenever this was possible, in other words, to reactions with only one substrate. Moreover, the multimolecular reactions (with more than one substrate or product) assumed to exhibit Michaelis–Menten kinetics in the reference model (RPPK and G3PDH) are left unchanged in the alternative models. All other multimolecular reactions are replaced with simplified kinetics. The reactions MurSynth, TrpSynth, and MetSynth were considered at steady-state (Chassagnole et al., 2002) and therefore the corresponding kinetic laws were not replaced in the alternative models. Among all the alternative models, the one...
where multimolecular reactions have been described by the convenience kinetics contains the highest number of kinetic parameters (115 as compared with 116 of the original model). This is followed by the model based on power-law rate laws that contains 110 parameters, the lin-log system with 96 and the GMA model with only 77 kinetic parameters (Table 2).

Parameter estimation can be performed through local and/or global methods (Mendes and Kell, 1998; Rodriguez-Fernandez et al., 2006). However, one of the major challenges in modeling large-scale dynamic systems is the existence of several local minima in the space of solutions. In this paper, we used an evolutionary programming method and its solution is then used as the starting point for a local search method (“Hooke and Jeeves”). To make sure that this method does not converge to a sub-optimal local minimum, 10 optimizations runs were performed with different random initial guesses.

After parameter estimation, we checked whether the alternative models are able to reproduce the same pseudo-experimental data used for parameter estimation. There exist a number of criteria to select among alternative candidate models. Here the \( f_{val} \) (Eq. (10)) and MRE (Eq. (11)) methods were used as measures of the quality of the fit for an estimated parameter set, which allows comparisons among different data sets and models. The results are summarized in Fig. 1. The mean and standard deviation of \( f_{val} \) were calculated and among the four models, the lin-log (\( f_{val} = 0.0341 \pm 0.00357 \)) achieved the best fits to the data followed by the convenience model (\( f_{val} = 0.272 \pm 0.138 \)), the GMA model (\( f_{val} = 0.591 \pm 0.288 \)), and the power-law model (\( f_{val} = 0.862 \pm 0.242 \)). Similar conclusions can be drawn from analysis of MRE (Fig. 1b).

To obtain time series data, the reference steady-state model was perturbed by increasing the extracellular glucose concentration at time zero from 0.0556 mM to 1.67 mM. The simulated time course data of the best fit solution for extracellular glucose, glyceraldehyde-3-phosphate, glucose-1-phosphate, fructose-1,6-bisphosphate, phosphoenolpyruvate, and pyruvate concentrations are shown in Fig. 2. In this figure we can observe that the discrepancies between the reference and alternative models were relatively small for most of the models in response to glucose addition, confirming also that the lin-log model gives the most accurate results and that it can successfully replace the full mechanistic model to represent the time course data along the 40 s. For all the remaining metabolites, there is also a good agreement between the reference and the lin-log model (data not shown).

![Fig. 1. Objective functions – (a) \( f_{val} \) and (b) mean relative error (MRE) – obtained during parameter identification for each alternative model from 10 independent estimation runs for each case.](image)

The average deviation (MRE) of the lin-log and convenience models to the reference simulated data for all metabolites was 6.37 \( \pm \) 0.87% and 18.21 \( \pm \) 2.71%, respectively. For the GMA it was 19.36 \( \pm \) 1.83% and for power-law 24.42 \( \pm \) 3.30%. The highest performance of the lin-log model for approximating enzyme kinetics is in line with a previous work from Heijnen (2005) for the single reaction level. In this work the authors describe the validity of lin-log kinetics for a single reaction and a higher performance was obtained when compared with other enzyme kinetics, such as the power-law formalism. Previous in silico and experimental studies have also shown a satisfactory performance of this non-linear kinetics upon large changes in metabolites concentrations and fluxes (Visser and Heijnen, 2003). More importantly, the lin-log model represents an option to simulate the dynamic behavior of the metabolic network with a lower number of kinetic parameters (96) compared with most of the other alternatives. Thus, the set-up of large-scale kinetic models based on this simplified model seems a promising approach to overcome the above-mentioned limitations.

A known limitation of the lin-log kinetics is that, for very small metabolite concentrations, it runs towards negative and the reaction rate is undefined. However, considering the homeostatic condition (i.e. steady-state) in the interior of the cell, this condition is unlikely to occur for metabolites in the E. coli central carbon metabolism. Another possible difficulty is the low sampling intervals of the metabolites required for parameter identification, but this is also a challenge of all the other kinetic models. For the parameter estimation, we assumed also that all the 18 metabolites are measurable. Even though this might be relevant at the present moment, the recent developments in high-throughput metabolomic methods that can be applied for such measurements will hopefully allow overcoming this issue (Buchholz et al., 2001; Soga et al., 2003). Finally, since lin-log models are obtained by a local approximation to a steady-state, it is likely that the quality of the results achieved in simulations deteriorates as we move away from this reference state. Taken these results together, the best performance of the lin-log model from a set of plausible candidates implied its selection for further analysis in this paper.

3.2. Performance of the Lin-Log Model

A requirement for a useful dynamic model is its stability. This can be achieved if all the eigenvalues of the Jacobian matrix for all parameter sets have negative real parts (Murray, 2002). To compare the stability of the lin-log model and the reference mechanistic model, we first computed the Jacobian matrix to determine all the eigenvalues for each complete ODEs system. If the real parts of the
Fig. 2. Comparison of simulated metabolite concentrations over time for extracellular glucose (Gluc. Ext.), glyceraldehyde-3-phosphate (GAP), glucose-1-phosphate (G1P), fructose-1,6-bisphosphate (FDP), phosphoenolpyruvate (PEP), and pyruvate (PYR) for the reference model (black solid line) and alternative models (GMA, gray solid line; convenience, gray dotted line; lin-log, black dotted line and power-law, gray dashed line) before and after a glucose impulse of 1.67 mM at time 0 s. Markers represent the experimental data for each metabolite.

Eigenvalues of both systems are negative than these models are stable and are able to return to the equilibrium after a perturbation in metabolite concentrations. The largest eigenvalue observed was $-0.0629 \text{s}^{-1}$ for the lin-log model and $-0.00853 \text{s}^{-1}$ for the reference model. Moreover, two complex eigenvalues were found for each model, indicating that the systems are able to oscillate, which corresponds to what can happen in real systems, as it has been shown experimentally (Buchholz et al., 2002).

In addition, the difference found in model stiffness ($4.0 \times 10^5$ for the reference model and $4.4 \times 10^5$ for the lin-log model) means that for the lin-log model the numerical methods used for simulation require slightly smaller time steps to obtain stable solutions of the system.

To validate the lin-log model, experiments with data sets different from the ones used for parameter estimation were performed. Predictions under new conditions were made with the best parameter set fixed. Thus, after a glucose impulse of 3.5 mM and 10 mM, the MRE index was calculated and values of 10.19% and 15.96% were obtained, respectively. The time series results for some metabolites from the glycolysis and pentose phosphate pathways after a glucose impulse of 3.5 mM are shown in Fig. 3. The behavior results indicate that the lin-log model, when compared with the reference model, has very good prediction levels during the 40 s time course for all the metabolites.

3.3. Sensitivity Analysis of the Model

Sensitivity analysis is also a tool for model validation and a measure of biological adequacy. This analysis quantified the effect that an infinitesimal change in the value of a parameter has on the steady-state values of the model, using usually methods of metabolic control analysis. In this study, however, we have focused...
on time-dependent sensitivity analysis, according to Eq. (12). High parameter sensitivities are often indicative that some parts of the system have not been adequately described. Here, we performed as example this analysis on the flux through the GAPDH reaction, one of the main reactions of glycolysis, for the period of 40 s. The time course results are presented in Fig. 4.

It is interesting to note the larger sensitivity with respect to a GAPDH parameter for the first 20 s and the relatively smaller effect of the other parameters. It is therefore interesting to focus on experiments on this period for fitting the kinetic parameters. Hence, with the sensitivity analysis we identified the most sensitive parameters and sampling time intervals, providing directions to future experimental design aimed at model refinement.

4. Conclusions

One of the major problems of setting-up large-scale dynamic models is the lack of kinetic data. The kinetic parameters are usually unknown, as well as the specific kinetic rate laws. Moreover, for a large number of reactions, the kinetic parameters are available in the literature only as general values obtained in in vitro conditions. There is therefore a need for alternative modeling approaches.

In this contribution we have build four alternative models combining Michaelis–Menten kinetics and approximated kinetic expressions, such as generalized mass action, convenience, lin-log, and power-law and the performance of these new models has been compared with a reference mechanistic model representing the E. coli central carbon metabolism.

Considering the good behavior performance obtained with the kinetic model composed of Michaelis–Menten and lin-log kinetics in comparison with the others, we conclude that this is a suitable approach for complex large-scale models where the exact rate laws are unknown. In combination with recent developments in time series data measurements, this approach should facilitate modeling of large-scale networks. As discussed above, care should be taken, however, if the conditions where the model is to be applied are far away from the reference state, as lin-log models are based on a local approximation assumption, and also when metabolite concentrations are close to zero.

Acknowledgments

Research supported by PhD grant SFRH/BD/25506/2005 from the Fundação para a Ciência e a Tecnologia (FCT) and the MIT-Portugal project “Bridging Systems and Synthetic Biology for the development of improved microbial cell factories” (MIT-Pt/BS-BB/0082/2008). The authors thank Dr. C. Chassagnole, who provided the experimental data set.

References


